# A COMPUTER CODE FOR

# HIGH ALTITUDE EMP

THESIS

GNE/PH/74-1

Terry C. Chapman
Capt USAF

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A relatively inexpensive computer code is developed to calculate the peak value of the electric field contained in an electromagnetic pulse generated by the gamma rays from a high altitude nuclear burst. The code is based on the Karzas and Latter theory for the production of Compton electrons and their interaction with the earth's magnetic field.

The code can be used to calculate the peak value of the electric field at a target anywhere on or above ground level,

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resulting from a nuclear burst above 60 km altitude with a gamma yield up to 60 tons. Either the direct or the ground reflected wave can be calculated. With special care, bursts up to 1 kt of gamma yield can be used.

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# A COMPUTER CODE FOR HIGH ALTITUDE EMP

THESIS

Presented to the Faculty of the School of Engineering
of the Air Force Institute of Technology
Air University
in Partial Fulfillment of the
Requirements for the Degree of
Master of Science

by

Terry C. Chapman, B.S.
Capt USAF
Graduate Nuclear Engineering

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## Preface

It is my pleasure to recognize several people who contributed in various ways to make this work possible.

I want to thank my advisor, Maj Carl T. Case. His patience and helpful suggestions were important factors to the successful conclusion of this work. In addition, I want to point out that the theoretical portion of this work is based largely on a series of lectures he gave while teaching the Electromagnetic Waves (EE 6.30) course during the summer quarter of 1973. His unusual ability to present difficult topics in a way that is easily understood by the student was the largest and most important contribution to the success of this work.

I want to thank Dr. Charles J. Bridgman for his suggestions and helpful comments made during the early stages of the work.

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Terry C. Chapman

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## Abstract

A relatively inexpensive computer code is developed to calculate the peak value of the electric field contained in an electromagnetic pulse generated by the gamma rays from a high altitude nuclear burst. The code is based on the Karzas and Latter theory for the production of Compton electrons and their interaction with the earth's magnetic field.

The code can be used to calculate the peak value of the electric field at a target anywhere on or above ground level, resulting from a nuclear burst above 60 km altitude with a gamma yield up to 60 tons. Either the direct or the ground reflected wave can be calculated. With special care, bursts up to 1 kt of gamma yield can be used.

# A COMPUTER CODE FOR HIGH ALTITUDE EMP

## I. Introduction

The effects of a nuclear environment on aerospace systems is an important factor in systems analysis. During the past few years several students have worked with Professor Bridgman at the Air Force Institute of Technology (AFIT) on a computer code to determine survivability of a system with known nuclear vulnerabilities from a variable nuclear threat. The AFIT survivability code capabilities include blast, thermal, x-ray, gamma ray, and neutron effects. The high altitude EMP code presented in this report is intended to be used in conjuction with the AFIT survivability code.

The EMP (electromagnetic pulse) from a nuclear weapon is usually considered to be a radiating electromagnetic wave of short duration containing many frequencies. However, the nuclear generated EMP was not studied seriously until a considerable time after the first nuclear explosion. At present there is a significant amount of work being done to model EMP generation and effects. For example the Air Force Weapons Laboratory (AFWL) and several civilian companies under contract to the USAF are working in the field.

There are several different types of EMP with distinctions made between the mechanisms which generate them. Kinsley (Ref 1) presents a comprehensive discussion of the various types of EMP. For example, a nuclear burst on the ground produces an EMP with different characteristics

than those from a high altitude burst. Also, nuclear burst products interacting directly with a system can produce an EMP within the system or even within the circuits of the system. This report considers only the EMP generated by high altitude burst gamma rays interacting with the atmosphere.

The high altitude EMP code developed in this report is based on the theory of Karzas and Latter (Ref 2). Briefly, the theory develops a model for the interaction of Compton electrons with the geomagnetic field. The Compton electrons are produced by prompt gamma radiation from the burst in a reasonably well defined region in the atmosphere. Several simplifications are made before arriving at the final equations.

Since several of the simplifications and assumptions used are implicit in the presentation of the theory, it is appropriate to list them here. Only one group of monoenergetic unscattered gamma rays are considered to produce Compton electrons. Each gamma which interacts is assumed to produce one and only one Compton electron initially traveling precisely in the radial direction. No angular distribution of Compton electrons is allowed. All Compton electrons are assumed to have the same energy. Curvature of the Earth's magnetic field is ignored. The electromagnetic fields are not self-consistent, that is, only the geomagnetic field is considered to affect the motion of the Compton electrons. Cascading of secondary electrons and recombination of ions is ignored. The low

frequency portion of the pulse is not considered. The Earth is assumed to be flat and the finite conductivity of ground is not considered. The burst is assumed to be far from the absorption region. Only gamma ray effects are considered.

Although the final model is somewhat restricted by these assumptions and simplifications, the end result is a relatively inexpensive computer code which gives a peak value of the electric field at any target point on or above the ground, which is an upper bound on the actual peak value.

Section II of this report develops the theory and derives the equations used in the code. Section III describes the calculational procedures used in the code. Section IV presents a sample of typical results and a study of input parameter variation. Section V is a discussion of the code's limitations and uses, with recommendations for possible improvements. Appendix A is a code user's guide. Appendix B is the detailed flow charts for the entire code. And finally Appendix C is a listing of the complete code.

# II. Theory

## Overview

The EMP problem is a problem in classic electromagnetic theory. A solution of Maxwell's equations is a solution of the problem. In this case it is necessary to model the current and charge densities generated by the gamma rays in the absorption region to obtain the sources and conductivity needed to solve Maxwell's equations.

Expressions for the current sources and conductivity are obtained in four steps. The transport of the gammas from the burst to the absorption region is used to obtain the number density of reacting gammas. This result is used with the models for the current and charge densities to obtain preliminary expressions. Then after considering the relativistic motion of the Compton electrons, the preliminary expressions are transformed to spherical coordinates.

After presenting Maxwell's equations in a convenient form, they are transformed to spherical coordinates and retarded time. A high frequency approximation is then made to arrive at the final equations.

## Electron Current and Density

Gamma Transport. Consider the geometry shown in Fig. 1. The nuclear burst occurs at the origin at time, t = 0. The gamma rays move to point r' in time t' and at that point and time interact to create Compton electrons. It is assumed

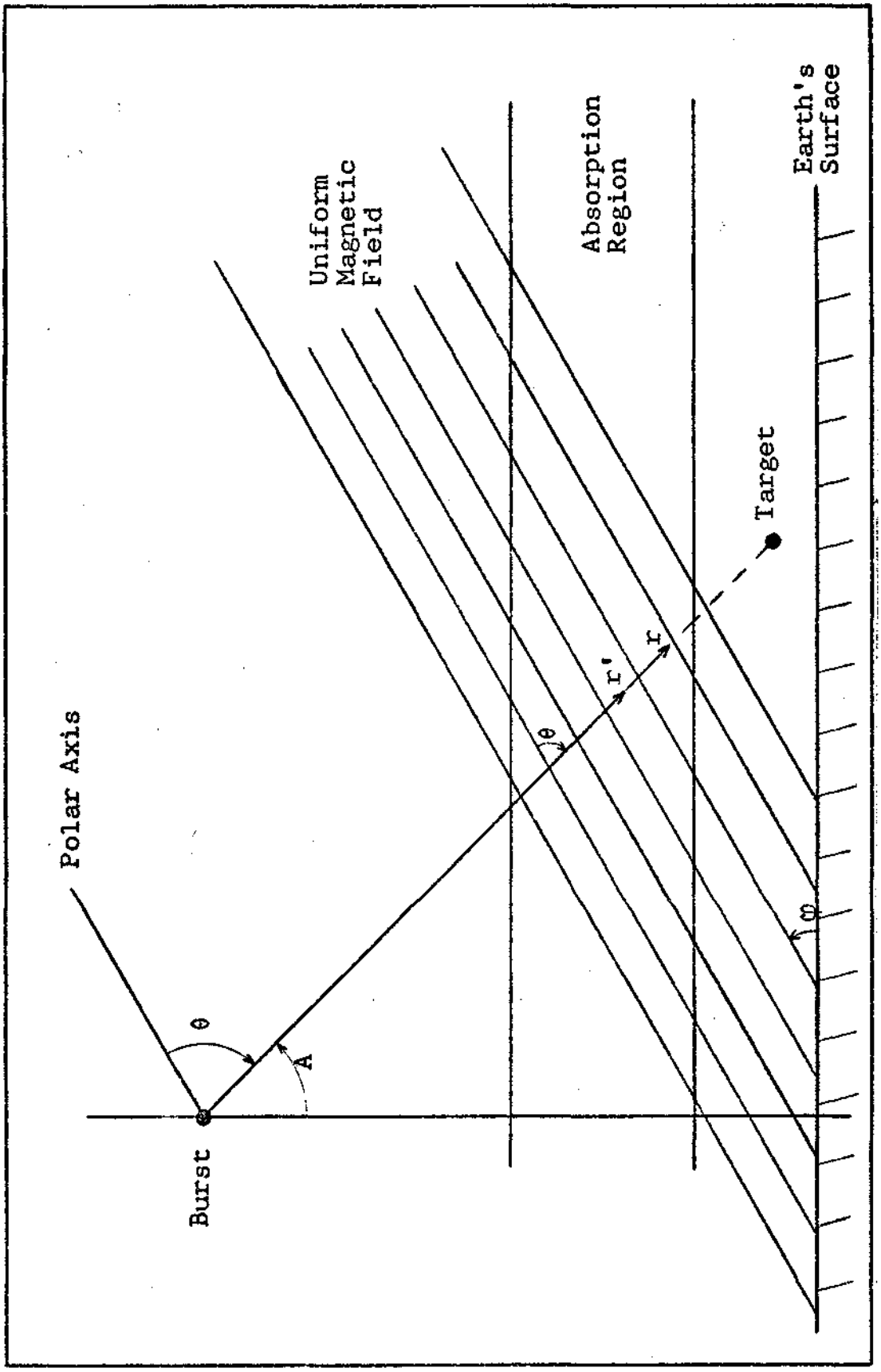



Fig. 1. Geometry of the Burst

that each gamma creates one and only one Compton electron traveling in the radial direction with the maximum Compton recoil energy.

The gamma ray emission rate can be taken as

$$\frac{dN(t)}{dt} = \frac{Y}{E} f(t) \tag{1}$$

where

N(t) = number of gamma rays emitted

Y = gamma ray yield of burst

E = mean energy of the gamma rays

f(t) = time dependence of the yield

and

$$\int_{-\infty}^{\infty} f(t)dt = 1 \tag{2}$$

The number density of gammas, g(r), which interact at a point, r, can be taken as

$$g(r) = \frac{Y}{E} \frac{\exp\left\{-\int_0^r \frac{dr'}{\lambda(r')}\right\}}{4\pi r^2 \lambda(r)} \tag{3}$$

where

$\lambda$ = mean free path for production of Compton electrons.

Electron Currents and Densities. The rate of production of primary (Compton) electron density, $n_{pri}$, is

$$\frac{dn_{pri}}{dt} = g(r)f(t - r/c) \tag{4}$$

Following the Karzas-Latter approach (Ref 2) it is assumed that the electrons maintain their initial speed, $V_0$, throughout their range, R, and then abruptly stop. Also, it is assumed that the secondary electrons are made at a uniform rate during the lifetime, $R/V_0$, of the Compton electrons. Therefore, the rate of production of secondary electron density, $n_{sec}$, is

$$\frac{dn_{sec}}{dt} = \left\{ \frac{E_{pri}/33ev}{R/V_0} \right\} n_{pri} = \frac{qV_0}{R} n_{pri} \qquad (5)$$

where

$E_{pri}$ = the initial energy of the Compton electrons

R = the range of the Compton electrons in air

q = $E_{pri}/33ev$

33ev = average ionization energy per molecule for air

$V_0$ = the speed of the Compton electrons

$R/V_0$ = the lifetime of the Compton electrons

Now consider the current resulting from the Compton electrons. The differential current is the charge times the velocity times the differential density of electrons. Hence

$$d\vec{J}^c = -e\vec{V}(t-t')g(r')f(t' - r'/c)dt' \qquad (6)$$

where

$\vec{V}(t-t')$ = velocity of the Compton electrons at time t which were created at time t'.

Putting (6) into integral form gives

$$\vec{J}^c = -e \int_{t-R/V_0}^{t} g(r')f(t' - r'/c)\vec{V}(t-t')dt' \qquad (7)$$

Now let

$$\tau' = t - t' \qquad (8a)$$

$$\tau = t - (r/c) \qquad (8b)$$

$$X(\tau') = X(\tau) = r - r' \qquad (8c)$$

Also note that

$$(r-r') << r \text{ or } r' \qquad (9)$$

for distant explosions (see Fig. 1). So,

$$g(r) \simeq g(r') \qquad (10)$$

Using Eqs (8), (9), and (10) in Eq (7) gives

$$\vec{J}^c = -eg(r) \int_0^{R/V_0} \vec{V}(\tau')f\left(\tau - \tau' + \frac{X(\tau')}{c}\right)d\tau' \qquad (11)$$

Using similar arguments,

$$n_{pri} = g(r) \int_0^{R/V_0} f\left(\tau - \tau' + \frac{X(\tau')}{c}\right) d\tau' \qquad (12)$$

And putting Eq (12) into Eq (5) yields

$$n_{sec} = \frac{qV_0}{R} \int_{-\infty}^{\tau} n_{pri}(\tau')d\tau'$$

$$= g(r) \frac{qV_0}{R} \int_{-\infty}^{\tau} \left[ \int_0^{R/V_0} f\left(\tau' - \tau'' + \frac{X(\tau'')}{c}\right) d\tau'' \right] d\tau' \quad (13)$$

Relativistic Electron Motion. Equations (11), (12), and (13) contain $r(\tau)$ and $X(\tau)$ which are not yet defined in an easily obtained form. The equation of motion for a Compton electron is

$$\frac{d}{dt}(m\gamma\vec{V}) = -e\vec{V}X\vec{B}_0 \quad (14)$$

where

$m$ = electron rest mass

$\gamma = [1-(V/c)^2]^{-1/2}$

$\vec{B}_0$ = earth's magnetic field = $B_0\hat{U}_z$

Again it is assumed that $V_0$ is constant throughout the electron's lifetime.

With $\omega = eB_0/m\gamma$ Eq (14) becomes

$$\frac{d}{d\tau}\vec{V}(\tau) = -\vec{V}(\tau)X\hat{U}_z\omega \quad (15)$$

Breaking Eq (15) into its rectangular components

$$\frac{dV_x}{d\tau} = -\omega V_y \quad (16a)$$

$$\frac{dV_y}{d\tau} = \omega V_x \tag{16b}$$

$$\frac{dV_z}{d\tau} = 0 \tag{16c}$$

A solution for this set of equations is

$$V_x = V_\perp \cos \omega\tau \tag{17a}$$

$$V_y = V_\perp \sin \omega\tau \tag{17b}$$

$$V_z = V_{||} \tag{17c}$$

where $V_\perp$ is the initial velocity component perpendicular to $\vec{B}_0$ and $V_{||}$ is the initial velocity component parallel to $\vec{B}_0$ and both are constants with respect to $\tau$.

Transformation to Spherical Coordinates. It is convenient to transform the above solution to a spherical coordinate system with its origin at the burst point. The transformation from rectangular to spherical coordinates is

$$V_r = V_x \sin\theta \cos\phi + V_y \sin\theta \sin\phi + V_z \cos\theta \tag{18a}$$

$$V_\theta = V_x \cos\theta \cos\phi + V_y \cos\theta \sin\phi - V_z \cos\theta \tag{18b}$$

$$V_\phi = -V_x \sin\phi + V_y \cos\phi \tag{18c}$$

Without loss of generality the coordinates can be chosen such that $\vec{V}$ lies in the X-Y plane, hence $\phi = 0$, and the transformation becomes

$$V_r = V_x \sin\theta + V_z \cos\theta \tag{19a}$$

$$V_\theta = V_x \cos\theta - V_z \sin\theta \tag{19b}$$

$$V_\phi = V_y \tag{19c}$$

Note that

$$V_\perp = V_0 \sin\theta \tag{20a}$$

$$V_{||} = V_0 \cos\theta \tag{20b}$$

Putting Eqs (17) and (20) into Eq (19) gives

$$V_r = V_0[\sin^2\theta \cos\omega\tau + \cos^2\theta] \tag{21a}$$

$$V_\theta = V_0[\cos\theta \sin\theta \cos\omega\tau - \sin\theta \cos\theta] \tag{21b}$$

$$V_\phi = V_0[\sin\theta \sin\omega\tau] \tag{21c}$$

Now $X(\tau)$ can be written as

$$X(\tau) = \int_0^\tau V_r d\tau = V_0[\sin^2\theta \frac{\sin\omega r}{\omega} + \tau \cos^2\theta] \tag{22}$$

Equations (21) and (22) substituted into Eq (11) give

$$J_r^c = -eg(r)V_0 \int_0^{R/V_0} f(T)[\cos^2\theta + \sin^2\theta \cos\omega\tau']d\tau' \tag{23}$$

$$J_\theta^c = -eg(r)V_0 \int_0^{R/V_0} f(T)[\sin\theta \cos\theta (\cos\omega\tau'-1)]d\tau' \tag{24}$$

$$J_\phi^c = -eg(r)V_0 \int_0^{R/V_0} f(T)[\sin\theta \sin\omega\tau']d\tau' \tag{25}$$

where

$$T = \tau - (1 - \beta \cos^2 \theta)\tau' + \beta \sin^2 \theta \frac{\sin \omega\tau'}{\omega} \quad (26a)$$

with

$$\beta = V_0/c \quad (26b)$$

Equations (23), (24), (25), and (26) provide the Compton currents within the absorption region in a form which can be used in the final field equations. In addition to the Compton currents, an expression for the conductivity within the absorption region is needed.

Equations (21) and (22) substituted into Eq (13) give

$$n_{sec}(\tau) = \frac{qV_0}{R} g(r) \int_{-\infty}^{\tau} \left[\int_0^{R/V_0} f(T')d\tau''\right]d\tau' \quad (27)$$

where

$$T' = \tau' - (1 - \beta \cos^2 \theta)\tau'' + \beta \sin^2 \theta \frac{\sin \omega\tau''}{\omega} \quad (28)$$

Consider the equation of motion for secondary electrons. Neglecting the $\vec{V}X\vec{B}_0$ term, which is small compared to the other terms (Ref 2) it is

$$m \frac{d\vec{V}}{dt} = -e\vec{E} - m\vec{V}\nu_c \quad (29)$$

where

$\nu_c$ = electron collision frequency.

These secondary electrons have velocities in the thermal region and are assumed to reach their maximum velocity instantly. In this case, Eq (29) becomes

$$\vec{V} = \frac{-e}{m\nu_c}\vec{E} \tag{30}$$

The current source from the secondary electrons is

$$\vec{J}^{sec} = -e\vec{V}(\tau)n_{sec}(\tau) = \frac{n_{sec}(\tau)}{m\nu_c}e^2\vec{E} \tag{31}$$

or in terms of conductivity

$$\vec{J}^{sec} = \sigma(\tau)\vec{E} \tag{32}$$

where

$$\sigma(\tau) = \frac{n_{sec}(\tau)}{m\nu_c}e^2 \tag{33}$$

Equations (32) and (33) provide the needed expressions for the conductivity.

Electromagnetic Fields from High Altitude Currents

Maxwell's Equations. Now that the Compton currents and the conductivity due to secondary electrons have been obtained, consider the field equations.

Maxwell's equations are

$$\vec{\nabla}\times\vec{E} = -\frac{\partial\vec{B}}{\partial t} \tag{34a}$$

$$\vec{\nabla}\times\vec{B} = \mu_0\vec{J} + \frac{1}{c^2}\frac{\partial\vec{E}}{\partial t} \tag{34b}$$

$$\vec{\nabla}\cdot\vec{E} = \frac{q_v}{\varepsilon_0} \tag{34c}$$

$$\vec{\nabla}\cdot\vec{B} = 0 \tag{34d}$$

where

$\vec{J}$ = total current density

$q_v$ = total charge density

Continuity of charge requires

$$\frac{\partial q_v}{\partial t} + \vec{\nabla}\cdot\vec{J} = 0 \tag{35}$$

It is convenient to combine the above equations into equations containing only $\vec{E}$ in one and only $\vec{B}$ in the other. Doing so gives

$$\left(\nabla^2 - \frac{1}{c^2}\frac{\partial^2}{\partial t^2}\right)\vec{E} = \mu_0\frac{\partial\vec{J}}{\partial t} + \frac{1}{\varepsilon_0}\vec{\nabla}q_v \tag{36}$$

$$\left(\nabla^2 - \frac{1}{c^2}\frac{\partial^2}{\partial t^2}\right)\vec{B} = -\mu_0\vec{\nabla}\times\vec{J} \tag{37}$$

Transformation to Spherical Coordinates and Retarded Time. Equations (36) and (37) will now be transformed to spherical coordinates and retarded time. Consider the transformation

$$\tau = t - r/c \tag{38a}$$

$$r' = r \tag{38b}$$

$$\theta' = \theta \tag{38c}$$

$$\phi' = \phi \tag{38d}$$

This is a spherical coordinate system where time is measured at each radial point in terms of the arrival of the bomb gamma rays at that point.

Using Eq (38) it is easily shown that

$$\frac{\partial}{\partial t} = \frac{\partial}{\partial \tau} \tag{39}$$

$$\frac{\partial}{\partial r} = \frac{\partial}{\partial r'} - \frac{1}{c}\frac{\partial}{\partial \tau} \tag{40}$$

$$\frac{\partial}{\partial \theta} = \frac{\partial}{\partial \theta'} \tag{41}$$

$$\frac{\partial}{\partial \phi} = \frac{\partial}{\partial \phi'} \tag{42}$$

Thus the operator

$$\frac{\partial}{\partial t}$$

transforms to

$$\frac{\partial}{\partial \tau}$$

and the operator

$$\vec{\nabla}$$

transforms to

$$\vec{\nabla} - \hat{U}_r \frac{1}{c} \frac{\partial}{\partial \tau}$$

Similarly, the operator

$$\nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2}$$

transforms to

$$\nabla^2 - \frac{2}{c} \frac{\partial}{\partial \tau} \frac{1}{r} \frac{\partial}{\partial r} r$$

Equation (36) now becomes

$$\left[ \nabla^2 - \frac{2}{c} \frac{1}{r} \frac{\partial}{\partial \tau} \frac{\partial}{\partial r} r \right] \vec{E} = \mu_0 \frac{\partial \vec{J}}{\partial \tau} + \frac{1}{\epsilon_0} \vec{\nabla} q_v - \hat{U}_r \frac{1}{c} \frac{\partial q_v}{\partial \tau} \quad (43)$$

and Eq (35) becomes

$$\frac{\partial q_v}{\partial \tau} = -\vec{\nabla} \cdot \vec{J} + \hat{U}_r \frac{1}{c} \frac{\partial}{\partial \tau} \cdot \vec{J} = -\vec{\nabla} \cdot \vec{J} + \frac{1}{c} \frac{\partial J_r}{\partial \tau} \quad (44)$$

Using Eq (44) in Eq (43) and rearranging gives

$$-\nabla^2 \vec{E} + \hat{U}_r \frac{1}{c\epsilon_0} \vec{\nabla} \cdot \vec{J} + \frac{1}{\epsilon_0} \vec{\nabla} q_v$$

$$+ \frac{\partial}{\partial \tau} \left[ \frac{2}{c} \frac{1}{r} \frac{\partial}{\partial \tau} (r\vec{E}) + \mu_0 (\vec{J} - \hat{U}_r J_r) \right] = 0 \quad (45)$$

Similarly, Eq (37) becomes

$$-\nabla^2\vec{B} + \mu_0\vec{\nabla}x\vec{J} + \frac{\partial}{\partial\tau}\left[\frac{2}{rc}\frac{\partial}{\partial r}(r\vec{B})\right]$$

$$+ \frac{\partial}{\partial\tau}\left[\frac{\mu_0}{c}(\hat{U}_\phi J_\phi - \hat{U}_\theta J_\theta)\right] = 0 \qquad (46)$$

High Frequency Approximation. Again, following the Karzas-Latter model, note that the variation of currents with distance is slow compared to variations with time and that the fields resulting from the transverse currents are rapidly varying in character, as are the currents themselves. Therefore, only the $\partial/\partial\tau$ terms are kept in the transverse field equations. Since the radial components do not propagate outside of the absorption region, they are not considered further in this report.

The transverse equations become

$$\frac{\partial}{\partial\tau}\left[\frac{2}{c}\frac{1}{r}\frac{\partial}{\partial r}(rE_\theta) + \mu_0 J_\theta\right] = 0 \qquad (47)$$

$$\frac{\partial}{\partial\tau}\left[\frac{2}{c}\frac{1}{r}\frac{\partial}{\partial r}(rE_\phi) + \mu_0 J_\phi\right] = 0 \qquad (48)$$

$$\frac{\partial}{\partial\tau}\left[\frac{2}{c}\frac{1}{r}\frac{\partial}{\partial r}(rB_\theta) - \frac{\mu_0}{c}J_\phi\right] = 0 \qquad (49)$$

$$\frac{\partial}{\partial\tau}\left[\frac{2}{c}\frac{1}{r}\frac{\partial}{\partial r}(rB_\phi) + \frac{\mu_0}{c}J_\theta\right] = 0 \qquad (50)$$

These equations are called the Karzas-Latter high frequency approximation for the EMP fields, and they are useful in the range $0 < \tau < 100$ shakes.

Integration with respect to time yields

$$\frac{2}{c}\frac{1}{r}\frac{\partial}{\partial r}(rE_\theta) + \mu_0 J_\theta = 0 \tag{51}$$

$$\frac{2}{c}\frac{1}{r}\frac{\partial}{\partial r}(rE_\phi) + \mu_0 J_\phi = 0$$

$$\frac{2}{c}\frac{1}{r}\frac{\partial}{\partial r}(rB_\theta) - \frac{\mu_0}{c} J_\phi = 0 \tag{53}$$

$$\frac{2}{c}\frac{1}{r}\frac{\partial}{\partial r}(rB_\phi) + \frac{\mu_0}{c} J_\theta = 0 \tag{54}$$

Recall that the total current density is

$$\vec{J} = \vec{J}^{pri} + \vec{J}^{sec} = \vec{J}^{c} + \sigma(\tau)\vec{E} \tag{55}$$

so Eqs (51) and (52) become

$$\frac{2}{c}\frac{1}{r}\frac{\partial}{\partial r}(rE_\theta) + \mu_0 J_\theta^c + \mu_0\sigma(\tau)E_\theta = 0 \tag{56}$$

$$\frac{2}{c}\frac{1}{r}\frac{\partial}{\partial r}(rE_\phi) + \mu_0 J_\phi^c + \mu_0\sigma(\tau)E_\phi = 0 \tag{57}$$

With the aid of a computer, it is now possible to obtain numerical solutions for the above equations which will yield a slightly high estimate of the peak value of the EMP pulse resulting from a high altitude burst.

Below the absorption region the Compton currents and the conductivity are zero. In this case, Eqs (56) and (57) have the following solutions:

$$E_\theta = C_1/r \tag{58}$$

$$E_\phi = C_2/r \tag{59}$$

where $C_1$ and $C_2$ are determined by the values of $E_\theta$, $E_\phi$, and r at the bottom of the absorption region.

# III. Code Description

## General Approach

Equations (56), (57), (58), and (59) were chosen as the simplest ones to solve numerically. Of course, Eqs (24), (25), (27), and (33) are used to obtain the Compton currents and conductivity needed to solve Eqs (56) and (57).

The B - field equations are not solved since

$$E = cB \tag{60}$$

can be used to obtain B once E is found. This relationship is based on the assumption that the EMP pulse is a spherical wave propagating in free space, below the absorption region.

The function used for the time dependence of the weapon yield is the one recommended by Pomranning (Ref 3).

$$f(\tau) = (1/N)\ \frac{(\alpha+\beta)\ \exp\ (\tau-\tau_0)}{\beta + \alpha\ \exp\ [(\alpha+\beta)(\tau-\tau_0)]} \tag{61}$$

where N is chosen such that

$$\int_0^\infty f(\tau)d\tau = 1 \tag{62}$$

and $\alpha > \beta$.

This function rises like $e^{\alpha\tau}$ for small $\tau$, falls like $e^{-\beta\tau}$ for large $\tau$, and has a single maximum at $\tau_0$.

Figure 2 presents a flow chart which is descriptive of the approach taken solving the equations. The top of the absorption region is assumed to be at 50 km altitude and the bottom of the absorption region is assumed to be

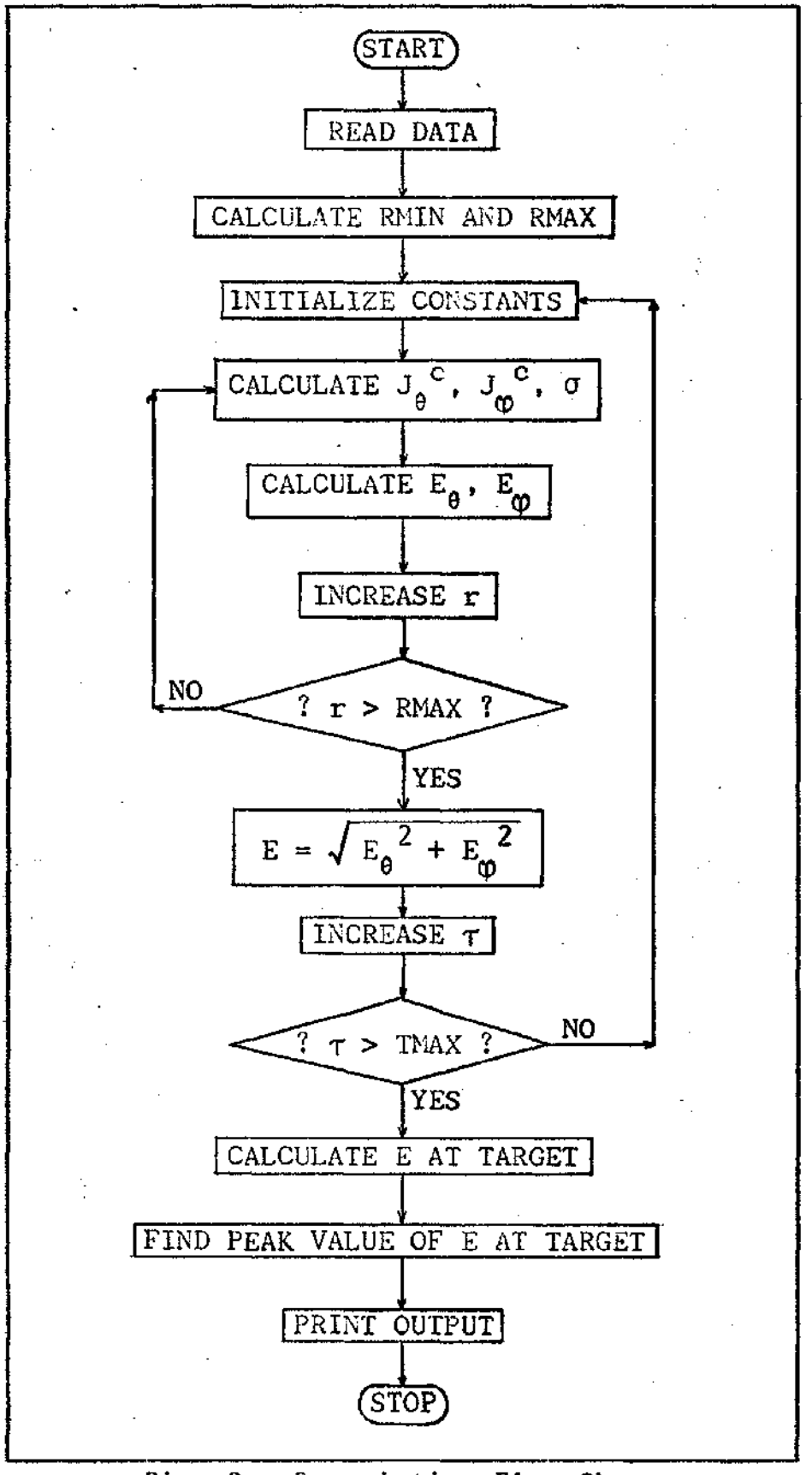



Fig. 2. Descriptive Flow Chart

at 20 km altitude. Calculations by Latter and LeLevier (Ref 4) indicate that 20 km to 50 km is the altitude where most of the prompt gamma ray energy is deposited.

Figure 3 depicts the target geometry. The value for RMIN is determined by the intersection of the line of sight with the 50 km altitude. The value for RMAX is determined by the intersection of the line of sight with the 20 km altitude. If the target is in the absorption region the target altitude determines RMAX for the direct wave calculation. These two values of r are the limits on the mesh in the r direction. The line of sight is divided into the desired number of steps along r for the integration on r in the absorption region.

The retarded time direction of the mesh is divided into 0.1 shake steps up to 10 shakes and then 1.0 shake steps on up to 100 shakes. Calculation can be stopped at any desired TMAX from 10 to 100 shakes, which is the upper limit of the usefulness of the high frequency approximation.

If the ground reflected wave is to be calculated, the mirror image of the target, below ground, is used to find the line of sight from the burst to the target. (Refer to Fig. 3.)

At r = RMIN all of the fields are assumed to be zero. For each $\tau$, equations (57) and (58) are integrated over r from RMIN to RMAX and the value of E at the bottom of the absorption region is stored. At each step in r, equations (24), (25), and (27) are numerically integrated. Then

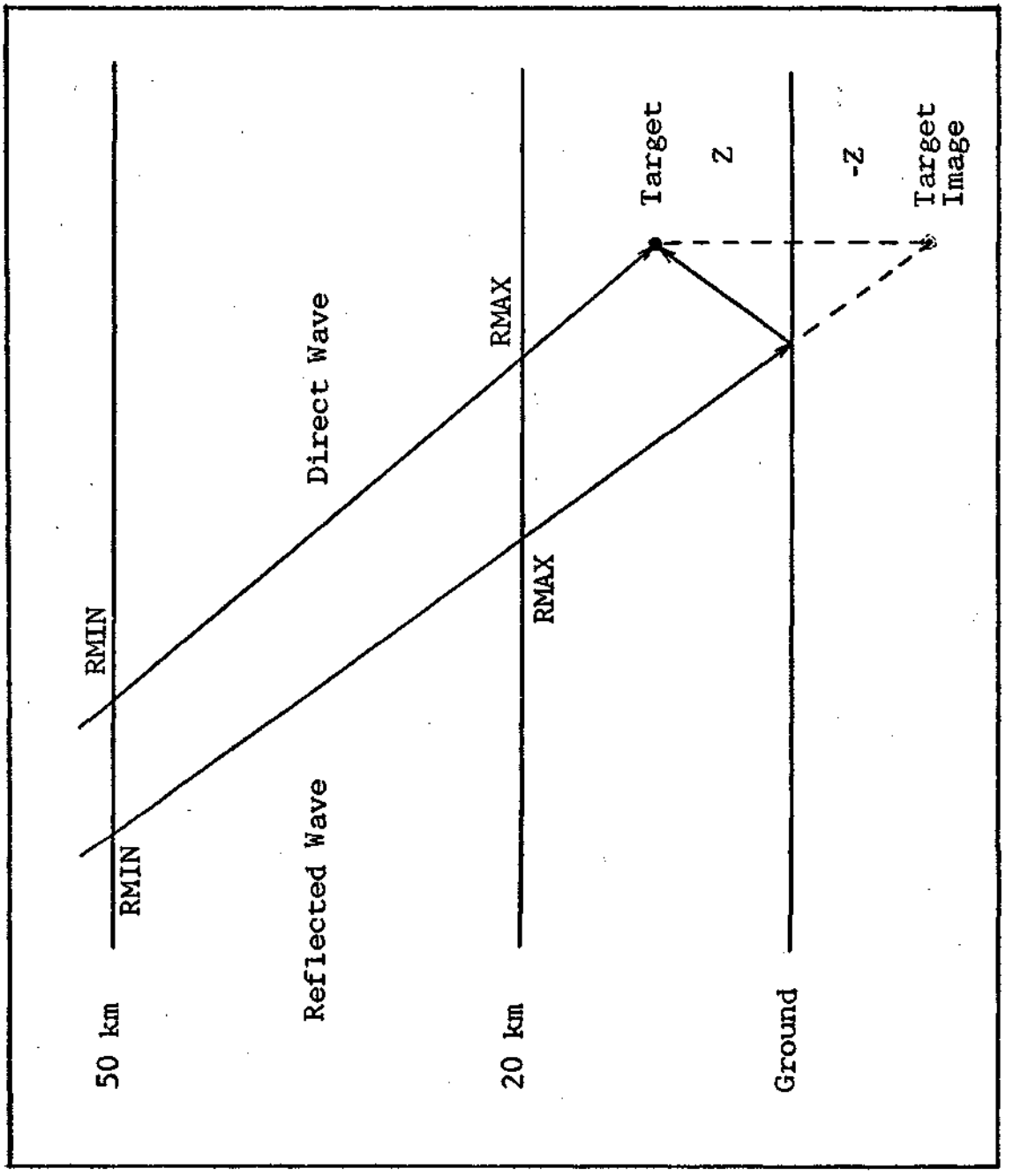



Fig. 3. Target Geometry

equations (58) and (59) are combined into

$$E = \frac{(RMAX)(E_{RMAX})}{r_{target}} \tag{63}$$

to find E at the target.

The E array is then searched to find the peak value before printing out the results.

Inputs

The code uses a right handed Cartesian coordinate system with the ground in the X-Y plane, the $\vec{B}_0$ vector in the Y-Z plane, and $\hat{j}$ pointing towards the equator. For example, in the northern hemisphere, $\hat{i}$ is magnetic west, $\hat{j}$ is magnetic south, and $\hat{k}$ is altitude. The origin of the coordinate system is always at ground zero, directly below the burst. Note that this coordinate system is not the same as the Cartesian systems used earlier.

Refering to the above coordinate system the target coordinates, (X,Y,Z), are read in using units of meters. If the reflected wave is to be calculated the altitude is read in as a negative number, (X,Y,-Z).

The height of the burst is read in using units of kilometers. The gamma yield of the burst is read in using units of kilotons.

The magnitude of the Earth's magnetic field is read in using units of webers per square meter. The dip angle ($\phi$ in Fig. 1) of the magnetic field is read in using units of degrees.

NDELR, the desired number of steps to be used in the integration over r in the absorption region, is read in as any integer in the closed interval [50, 500].

TMAX, the retarded time where calculations are to be stopped, is read in, using units of shakes, as any integer in the closed interval [10, 100].

Preliminary Calculations

Before starting the numerical integrations, the code performs several preliminary calculations. The input data is converted to MKS units. The reflected wave is used whenever Z is greater than 49 km or less than 0. The target coordinates are transformed to a spherical coordinate system with the burst at the origin and the polar axis parallel to $\vec{B}_0$. The line of sight intersections with the absorption region are determined. And finally, the constant angles required by the code, $\theta$ and A, (see Fig. 1) are calculated.

Calculation of Compton Currents and Conductivity

The two Compton currents, $J_\theta^c$ and $J_\phi^c$ are calculated at each r, $\tau$ mesh point by numerically integrating equations (24) and (25). The step size used is 0.1 times the Compton lifetime, $R/V_0$. The integration itself is done using the $4^{th}$ order Runge-Kutta method (Ref 5). It should be noted that both the mean free path for Compton interaction and the Compton lifetime are exponentially scaled from sea

level values using a 7 km scale height. However, the Compton lifetime is not allowed to be greater than 100 shakes, since this is the maximum time of interest.

Monoenergetic gammas of energy 1.5 Mev are assumed. The most energetic Compton electrons resulting from 1.5 Mev gammas have a speed of $2.88\ (10)^8$ m/sec. Therefore $V_0 = 2.88\ (10)^8$ m/sec.

Since the integration on $\tau''$ in equation (27) is also over the Compton lifetime, this integration is carried out simultaneously with the Compton current integrations. Again, the $4^{th}$ order Runge-Kutta method is used. It is broken into two parts, one for $-\infty < \tau' < 0$ and the other for $0 < \tau' < \tau$. In this case, $-\infty$ is defined to be the time when the first gamma ray reached the top of the absorption region, since no secondaries can be produced before that time.

The integration on $\tau'$ in equations (27) is also broken into two parts, one for $-\infty < \tau' < 0$ and the other for $0 < \tau' < \tau$. In the first case, integration is started at $\tau' = 0$ and proceeds to $\tau' = -(r\text{-RMIN})/V_0$ in steps of $\Delta\tau' = -\Delta r/V_0$. In the second case, integration is started at $\tau' = 0$ and proceeds to $\tau' = \tau$ in steps of $\Delta\tau' = \Delta\tau$. In both cases, simple step integration is used. That is

$$\int f(\tau')d\tau' = \sum_{\text{all } i} (\Delta\tau_i')[f(\tau_i')] \qquad (64)$$

The integration over $\tau'$ is carried out parallel to the integration of (56) and (57) over r (using space as a pseudo retarded time) and simultaneously with the increase in $\tau$ as the space integrations are repeated for each new $\tau$.

This rather involved approach to solving equation (27) is necessary to save running time. A direct approach, with separate integrations, would at least triple or quadruple the total running time required for execution of the code.

Integration of the Field Equations

For each $\tau$, equations (56) and (57) are integrated from r = RMIN to r = RMAX in steps of $\Delta r$ = (RMAX-RMIN)/NDELR using the $4^{th}$ order Runge-Kutta method. Then the magnitude of E is found from the two components and the result is stored in the E array. $\tau$ is increased by $\Delta\tau$ and the whole process is repeated until $\tau$ reaches TMAX.

On completion of the iterations, each member of the E array is multiplied by $RMAX/r_{target}$ (equation 62). Then the E array is searched to find the peak value.

Outputs

There are several output options available in the code. The basic output it:

1. Gamma yield and altitude of burst.
2. Target coordinates from ground zero.
3. Distance from burst to target.
4. A message indicating whether the direct or the reflected wave is being calculated.

5. The time period covered by the calculation.

6. The time when the peak value occured.

7. The peak value of E at the target.

8. The $\tau$ and E arrays.

In addition, a linear and a log-log plot of $E(\tau)$ can be obtained. Also, a listing of the values of E at the bottom of the absorption region for each $\tau$ can be obtained. Either or both of these two options can be added to the basic output.

## IV. Results and Input Parameter Variation

The output from a typical run is shown in Fig. 4. The $E(\tau)$ calculated during the run is shown in Fig. 5. The input data for this run was:

| | | |
|---|---|---|
| X | = 0 meters | (65a) |
| Y | = 0 meters | (65b) |
| Z | = 0 meters | (65c) |
| HOB | = 100 km | (65d) |
| $Y_Y$ | = .001 kt | (65e) |
| $B_0$ | = $2(10)^{-5}$ wb/m$^2$ | (65f) |
| Dip Angle | = 20° | (65g) |
| NDELR | = 50 | (65h) |
| TMAX | = 20 shakes | (65i) |

The CDC 6600 Computer required 191 sec and $33000_8$ words of central memory to execute this run.

The peak value of E, 6400 V/m, obtained in this run compares favorably with Karzas-Latter's order of magnitude estimate of $10^4$ V/m (Ref 2) from similar input data.

In order to gain a better knowledge of the operating capabilities of the code, the effect of varying input parameters one at a time was studied. The basic set of parameters used was:

```
THE BURST WITH GAMMA YIELD OF 1.000E-03 KILOTONS
IS AT AN ALTITUDE OF 1.000E+02 KILOMETERS.

THE TARGET IS AT COORDINATES      0.              0.              0.
WHICH IS 1.000E+05 METERS FROM THE BURST



DIRECT WAVE IS BEING CALCULATED



ITERATION TERMINATED AFTER 20.0 SHAKES



PEAK OCCURRED AT  2.1 SHAKES



* * * * * * * * * * * * * * * * * * * * * * * * * * * *
* PEAK EFIELD AT TARGET IS  6.448E+03 VOLTS/METER *
* * * * * * * * * * * * * * * * * * * * * * * * * * * *
```

Fig. 4. Output from a Typical Run

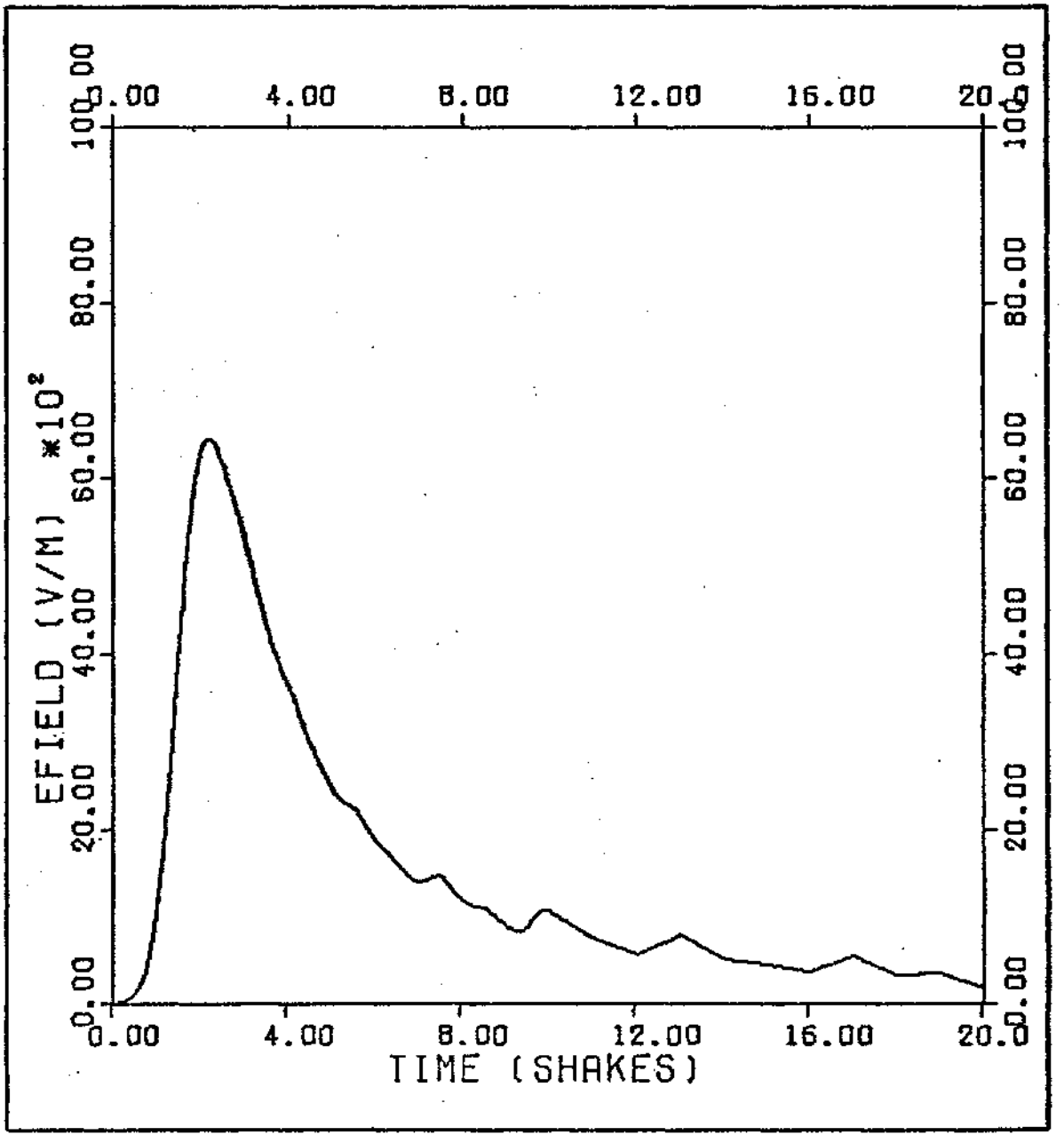



Fig. 5. Plot of E(τ) at target from a typical run

$$X = 0 \text{ meters} \tag{66a}$$

$$Y = 0 \text{ meters} \tag{66b}$$

$$Z = 0 \text{ meters} \tag{66c}$$

$$HOB = 100 \text{ km} \tag{66d}$$

$$Y_Y = .001 \text{ kt} \tag{66e}$$

Each of the above parameters was systematically varied while holding the others constant. The other inputs were held constant at the values shown in equations (65).

The results of the variation in X are shown in Fig. 6. Since the X axis is perpendicular to the magnetic field the symmetry about X = 0 is expected. The decrease in peak value of E for increasing distance from ground zero is due to the increasing distance from the burst.

The results of the variation in Y are shown in Fig. 7. Here the peak values of E depend on the angle between $\vec{r}$ and $\vec{B}_0$, $\theta$. When $\theta = 180°$ (A = -70° and Y = -275 km) the peak E drops to zero. The maximum peak E is skewed toward A = 20° ($\theta = 90°$ and Y = 36 km). The maximum is not exactly at A = 20° because of the increased distance from the burst. These characteristics are expected since an electron moving perpendicular to the magnetic field would feel the strongest acceleration from it while an electron moving parallel to the magnetic field would feel no acceleration at all.

The results of variation in Z are shown in Fig. 8. In this case, both the direct and the reflected waves were calculated at each point below the top of the absorption

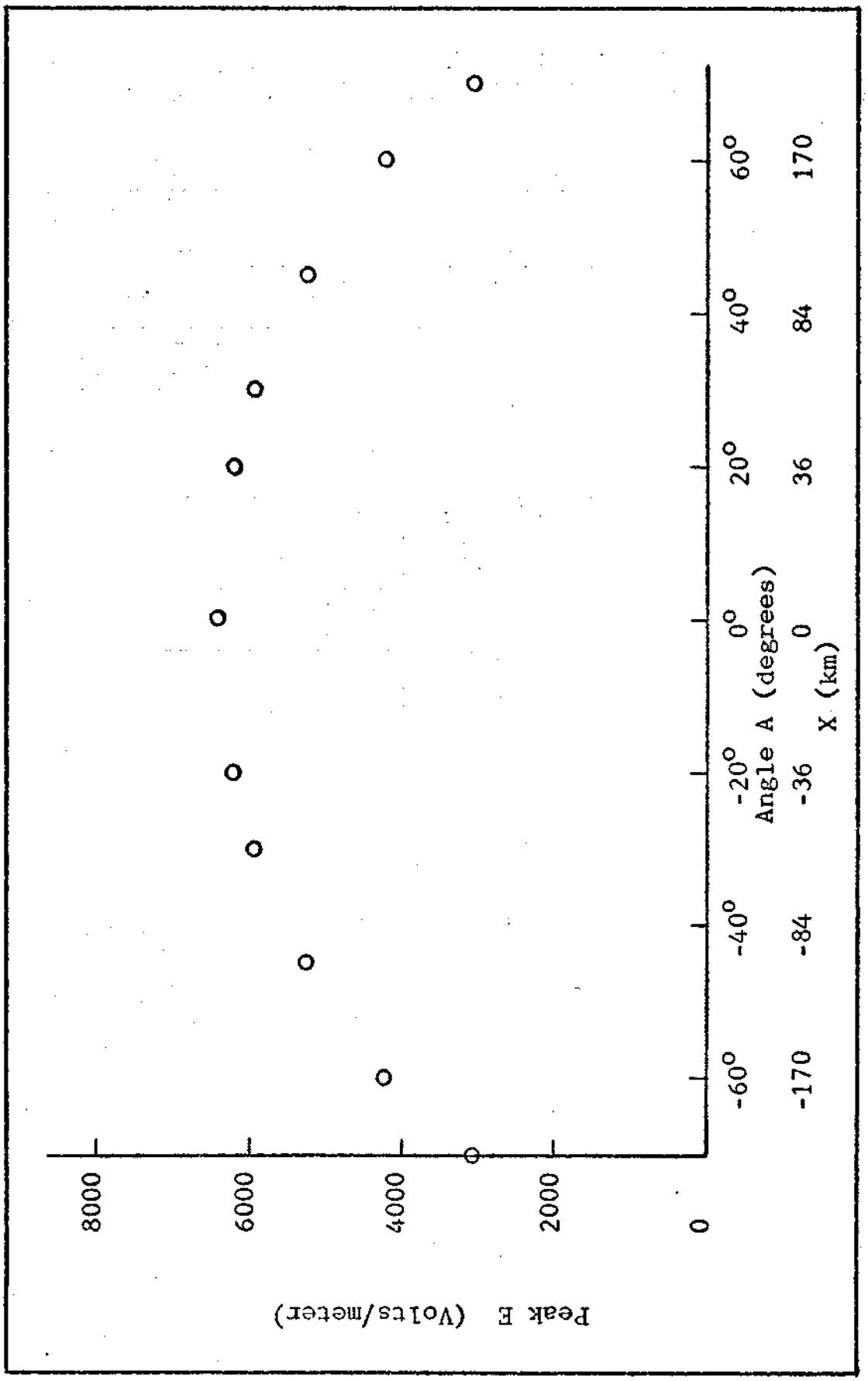



Fig. 6. Variation in the X Direction (Y=0, Z=0, HOB=100km, $Y_\gamma$=0.001kt)

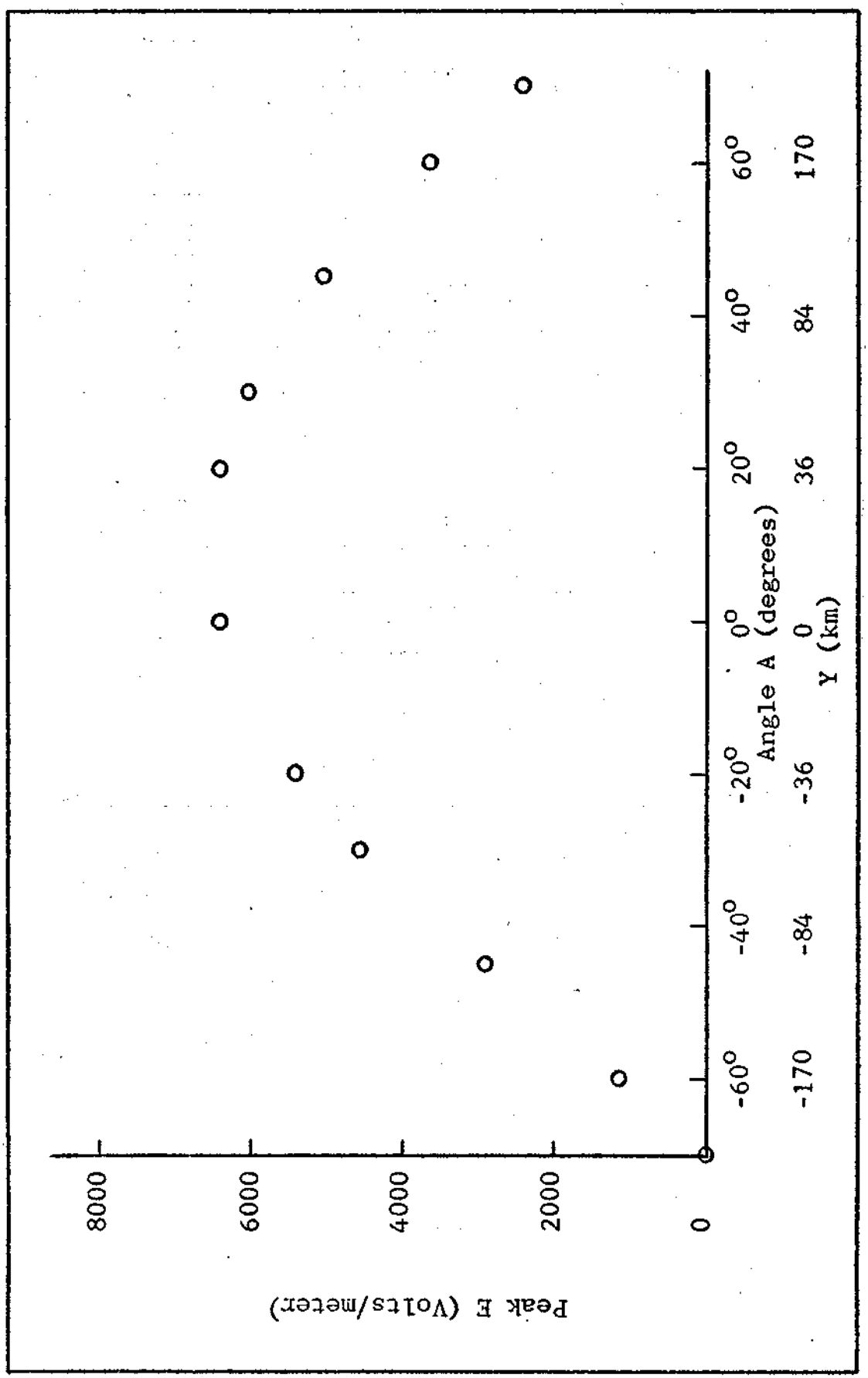



Fig. 7. Variation in Y direction (X=0, Z=0, HOB=100km, $Y_Y$=.001kt)

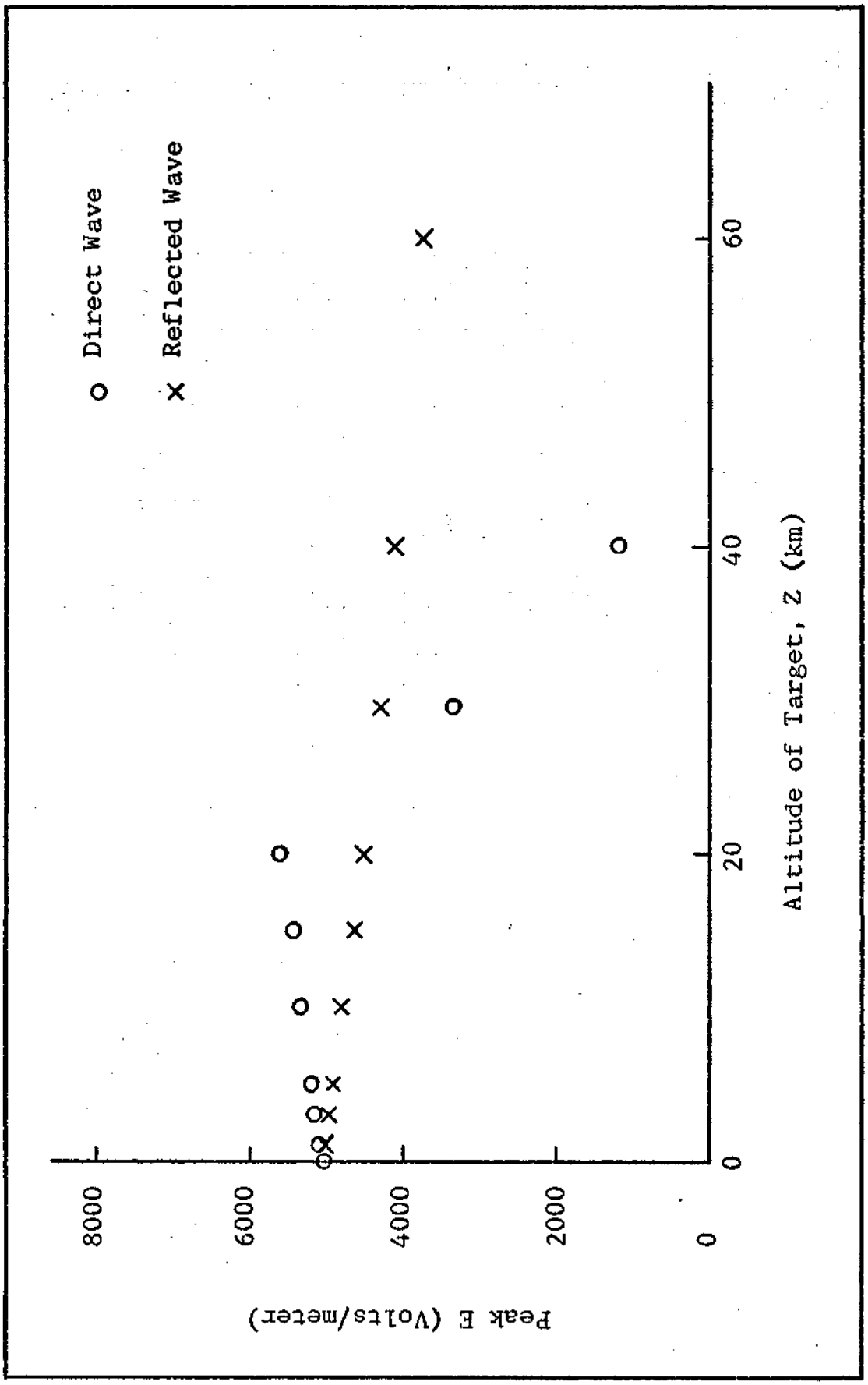



Fig. 8. Variation in Z Direction (X=0, Y=+100km, $Y_\gamma$=.001kt, HOB=100km)

region. Note that Y = 100 km for these runs. As expected, the direct wave falls off rapidly as the target altitude passes through the absorption region, since less of the absorption region contributes to the wave with each increase in altitude. The crossover point where the reflected wave becomes the largest occured at 25 km in this case. Above ground zero the crossover point was 29.4 km. The altitude of the crossover point is both yield and geometry dependent. It is necessary for the user to calculate both waves whenever there is any doubt which one is the largest.

The reflected wave calculation assumes 100% reflection from the ground and no attenuation in the absorption region or the ionosphere. These assumptions are reasonable if it is recalled that only the high frequency component is being considered and that it requires at least

$$\frac{40 \text{ km}}{3(10)^8 \text{m/sec}} = 133 \ \mu \text{ sec} \qquad (67)$$

for the wave to leave the absorption region, reach the earth, be reflected, and return to the absorption region. This length of time is enough for a significant number of the free electrons to recombine and reduce the effective conductivity of the absorption region.

The results of variation in HOB are shown in Fig. 9. For all values of HOB attempted below 60 km the code went unstable. Infinite values for E were obtained which resulted in abnormal termination of the calculations. This is

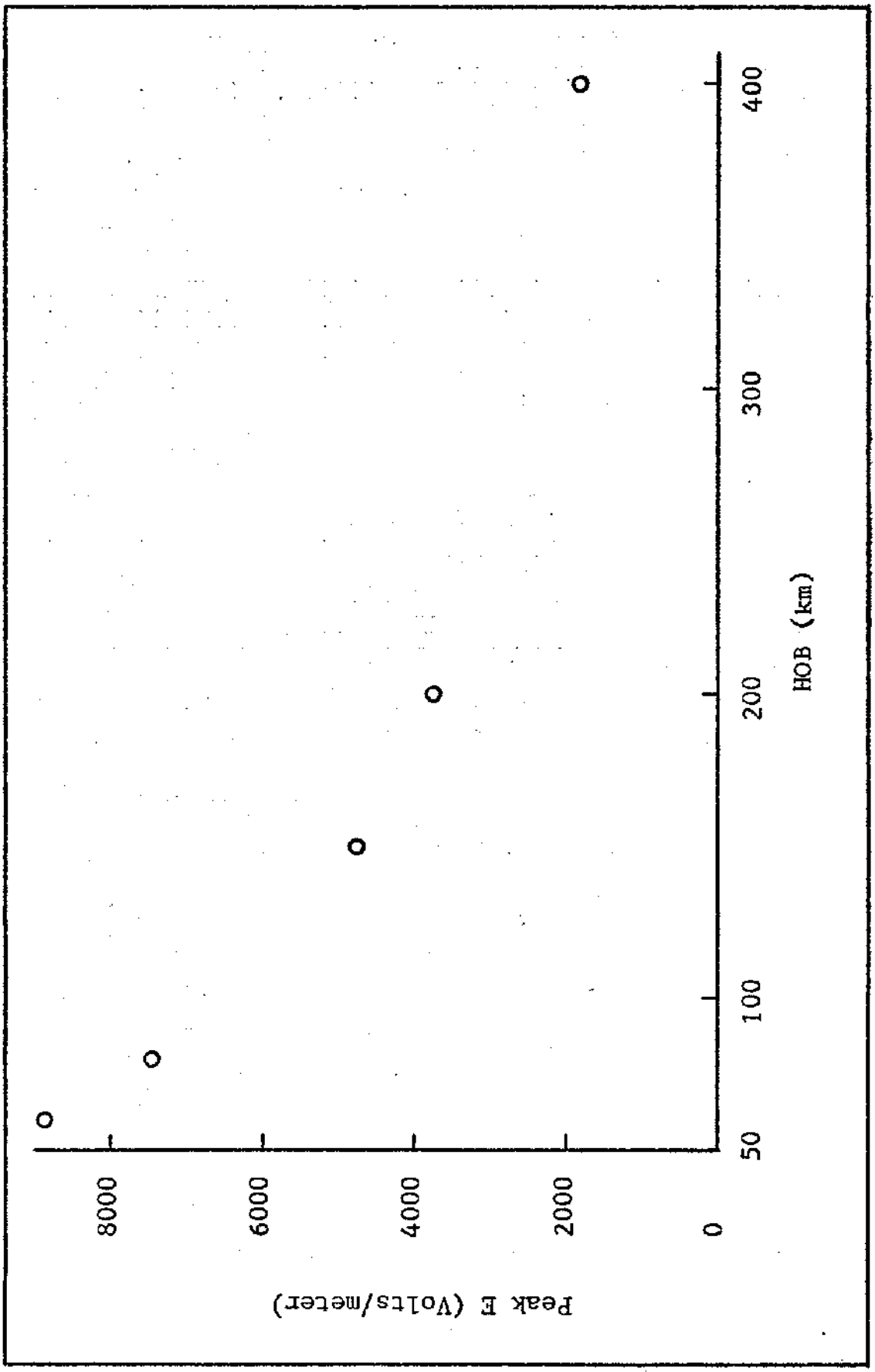



Fig. 9. Variation in Height of Burst (X=0, Y=0, Z=0, $Y_Y$=0.001kt)

expected since the burst is assumed to be distant from the absorption region (equations 9 and 10).

The results of variation in gamma yield are shown in Fig. 10. For all gamma yields attempted above 60 tons the code went unstable, giving infinite values for E. However, the instability always occured at times later than the natural peak value of E. For example, with 80 tons of gamma yield, the natural peak occured at 1 shake and the instability occured at 10 shakes. By using the natural peak value and ignoring the instability, reasonable values for peak E were obtained up to 1 kt of gamma yield.

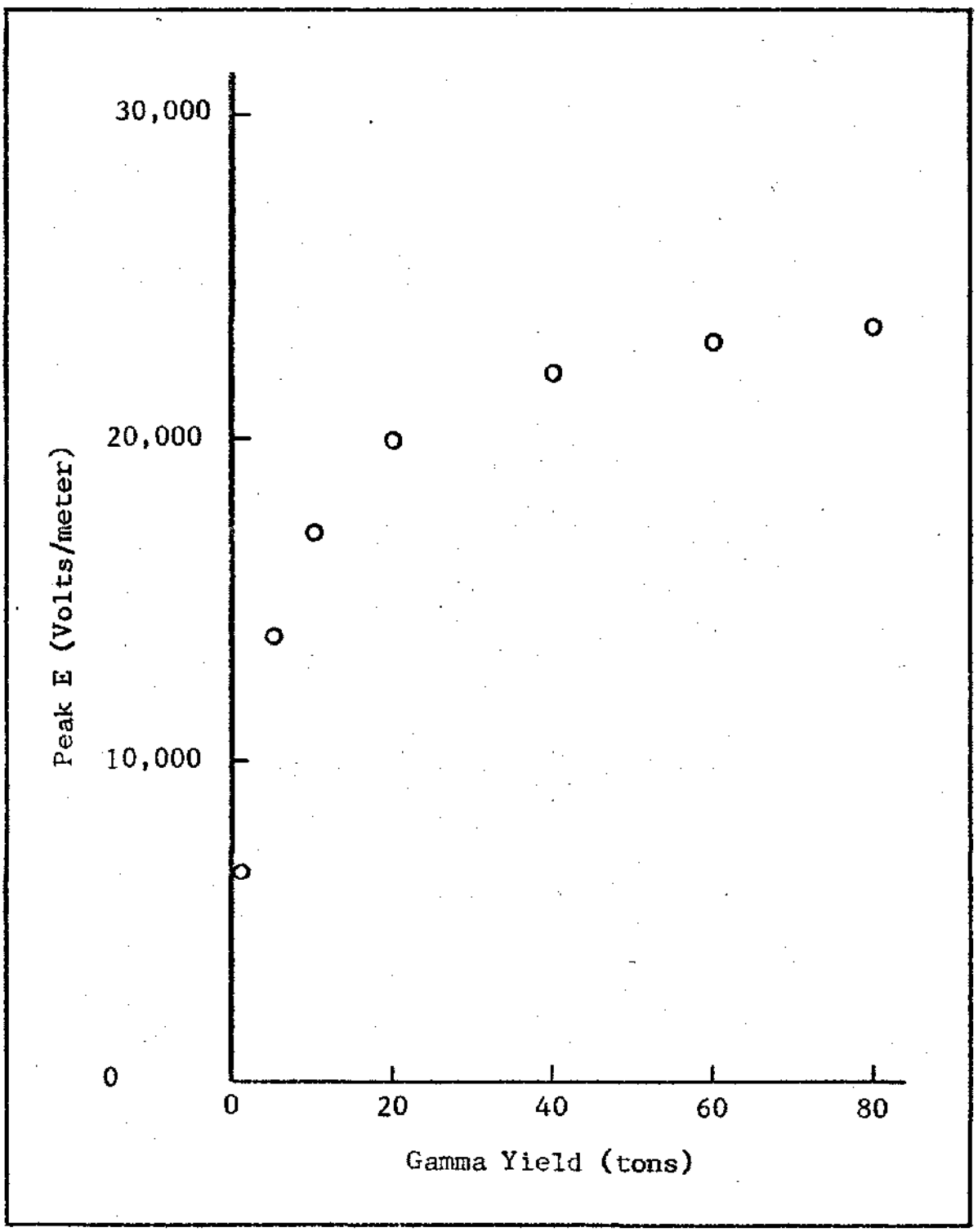



Fig. 10. Variation in Gamma Yield (X=0, Y=0, Z=0, HOB=100km)

# V. Discussion and Recommendations

## Limitations

Most of the limitations of the code are inherent in the model upon which it is based. Approximations such as a flat earth, a uniform magnetic field, and constant speed Compton electrons can be improved only by changing the model. In addition, the effect of the self generated electromagnetic fields on the motion of the Compton electrons is ignored, as is recombination of both primary and secondary electrons. The possibility of a single gamma ray interacting to produce more than one Compton electron is not allowed. In the absorption region the contribution of the non-propagating radial component of the electric field is neglected. Also, the model is not easily adapted to multi-group gamma transport, or to multiple burst calculations.

The code calculates only the effect of the gamma rays. The user must keep in mind that X-ray generated EMP becomes important for bursts above 100 km.

The code does not account for the increase in altitude of the absorption region for slant angles (angle A in Fig. 1) greater than 60° which is indicated by Latter and LeLevier (Ref 4).

Since 97% of the running time of the code is used for numerical iteration it is not practical to adapt the code to run more than one target at a time. Two targets would

merely double the running time, so it is simpler to just make two runs. Typical requirements are 200 seconds running time with $33000_8$ words of central memory on the CDC 6600 computer using NDELR = 50 and TMAX = 20 shakes.

Uses

The code can be used to calculate the peak value of the E field at a target, anywhere on or above ground level, resulting from a nuclear burst above 60 km altitude with a gamma yield up to 60 tons. Either the direct or the ground reflected wave can be calculated. With special care, bursts up to 1 kt of gamma yield can be used.

Recommendations

In the interest of accuracy, the targets should be located such that the slant angle, A, is between -60° and +60°.

By accepting a much longer running time the accuracy and hopefully, the stability of the code could be improved by using a smaller step size in the integration of the Compton current equations. Reducing the step size from one tenth of the Compton lifetime to one shake would require approximately ten times as much running time as the code presently requires. This possibility should be investigated further to determine the optimum step size for obtaining the best relationship between accuracy and running time.

Another possibility for increasing the accuracy and stability of the code is to reduce the step size in r. The present code has the capability of dividing the absorption region into 500 steps in r along the line of sight. Of course, the running time required for 500 steps is ten times that required for 50 steps. A modification of the code to allow more than 500 steps would increase the amount of computer core required as well as increasing the running time. This provides another area for investigation to determine the best trade off point between accuracy and running cost.

These two possibilities could be investigated with minor modifications to the present code. However, the computer time required would be considerable.

In addition, there are numerous possibilities for improvements in the model itself. Some of the more important ones are;

Using multigroup gamma transport.

Using multigroup Compton electrons.

Allowing angular distribution of Compton electrons.

Using self consistent electromagnetic fields.

Including the low frequency components.

Each of these would require major modifications to the present code.

## Bibliography

1. Kinsley, O.V. Introduction to the Electromagnetic Pulse, Wright-Patterson AFB: Air Force Institute of Technology, March 1971. (GNE/PH/71-4).

2. Karzas, W. J. and R. Latter. "Detection of the Electromagnetic Radiation from Nuclear Explosions in Space", Physical Review, Vol 137, No. 5B. pages 1369-1378, March 8, 1965. (Also published as EMP Theoretical Note 40).

3. Pomranning, G. C. "Early Time Air Fireball Model for a Near-Surface Burst", DNA 3029T, March 1973.

4. Latter, R. and R. E. LeLevier. "Detection of Ionization Effects from Nuclear Explosions in Space", Journal of Geophysical Research, Vol. 68, No. 6, March 15, 1963.

5. Wylie, C. R. Jr. Advanced Engineering Mathematics, New York: McGraw-Hill Book Co. 1966. (Third Edition).

6. Lecture Notes, Electromagnetic Waves, EE 6.30, Air Force Institute of Technology, Wright-Patterson AFB, Summer, 1973. (Course taught by Maj. Carl T. Case.)

# Appendix A

## EMP Code User's Guide

## EMP Code User's Guide

The code is run the same as any other Fortran Extended program, but due to the running time it should be converted to binary form before execution. The plotting subroutine requires an on-line plotter and both linear and log plotting library subroutines.

The input data is read in the following order:

Data card #1, using FORMAT (7F10.0, 215), contains;

- X,Y,Z — The target coordinates in meters
- HOB — The height of the burst in kilometers (60 km $\leq$ HOB)
- GAMYLD — The gamma yield in kilotons (GAMYLD $\leq$ 1 kt)
- BFIELD — The Earth's magnetic field in $wb/m^2$
- BANGLE — The magnetic field dip angle in degrees
- NDELR — The number of steps in r taken through the absorption region (50 $\leq$ NDELR $\leq$ 500)
- OUT — The output control parameter

Data card #2, using FORMAT (13), contains;

- ITER — The time period covered by the iterations in shakes (10 $\leq$ ITER $\leq$ 100) (ITER = TMAX)

Data card #3, using FORMAT (4F10.0), contains;

- A — Pomranning constant $\alpha$ in inverse shakes
- B — Pomranning constant $\beta$ in inverse shakes
- RN — Pomranning constant N in shakes
- TO — Pomranning constant $\tau_0$ in shakes

Default values are provided for BANGLE, BFIELD, and NDELR. They are 40°, 0.00002 wb/$m^2$, and 50 respectively. If these default values are desired, zero must be punched in their respective card fields.

The ground reflected wave at the target is obtained by reading in the target altitude, Z, as a negative number. For any target within the absorption region, both the direct and the ground reflected wave should be calculated to determine which one is the strongest.

For values of GAMYLD between 0.06 kilotons and 1.0 kilotons the code will most likely go unstable. This instability occurs after the real peak has been calculated, but the peak value printed out may not be the real peak. Since execution is terminated when the field becomes greater than 1E15 V/m, the array search can result in a false peak value. In this case, the arry itself (or the plot) can be used to determine the real peak value.

Increasing NDELR makes the step size in r through the absorption region smaller and the calculation becomes more accurate. However, total running time varies directly with changes in NDELR. For example, using NDELR = 100 instead of NDELR = 50 will approximately double the running time required for NDELR = 50.

There are four output options provided. Option 0 prints out the informative messages, the calculated peak value at the target, the E array, and the $\tau$ array. Option 1 adds a linear plot of the first 20 shakes and a log-log

plot of 100 shakes of E as a function of $\tau$ at the target. Option 2 includes both Option 0 and Option 1 and adds a printout of E and $\sigma$ as a function of $\tau$ at the bottom of the absorption region. Option 3 deletes the plots from Option 2. The last two options are primarily for debugging since a partial printout is made for each completed iteration even if execution is terminated before the iterations are completed. The first two options are best for production runs.

The only requirements on the Pomranning constants are N must be chosen such that equations (61) and (62) are satisfied, all of them must be positive, and $\alpha > \beta$.

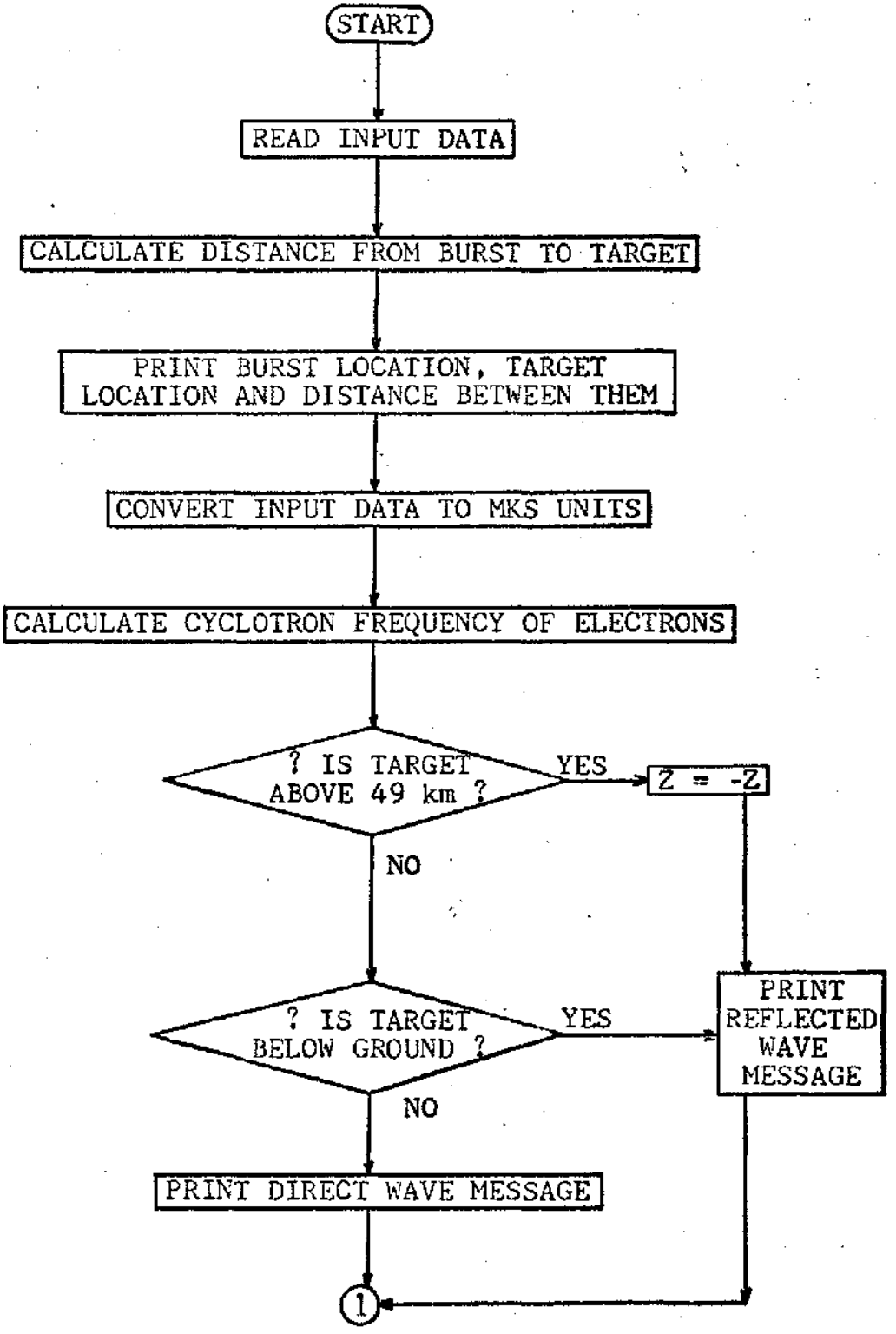
Increasing ITER also increases the running time. For ITER = 10 shakes, running time is approximately 180 seconds on the CDC 6600 computer. For ITER = 100 shakes, running time is approximately 340 seconds. A good compromise, which gives nice looking plots, is ITER = 20 shakes with a running time of approximately 200 seconds.

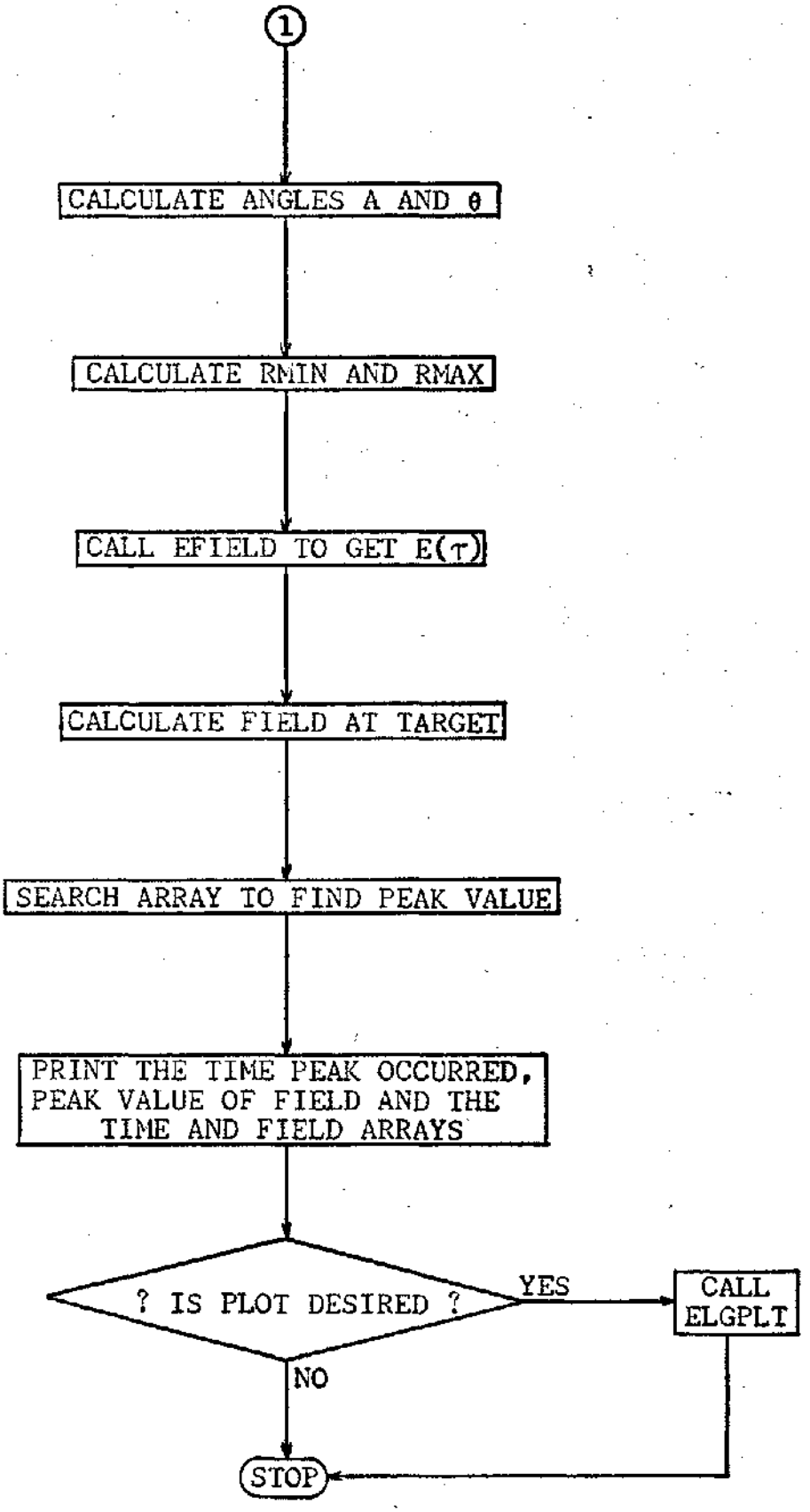
In binary form, the code requires $33000_8$ words of core on the CDC 6600 computer.

# Appendix B

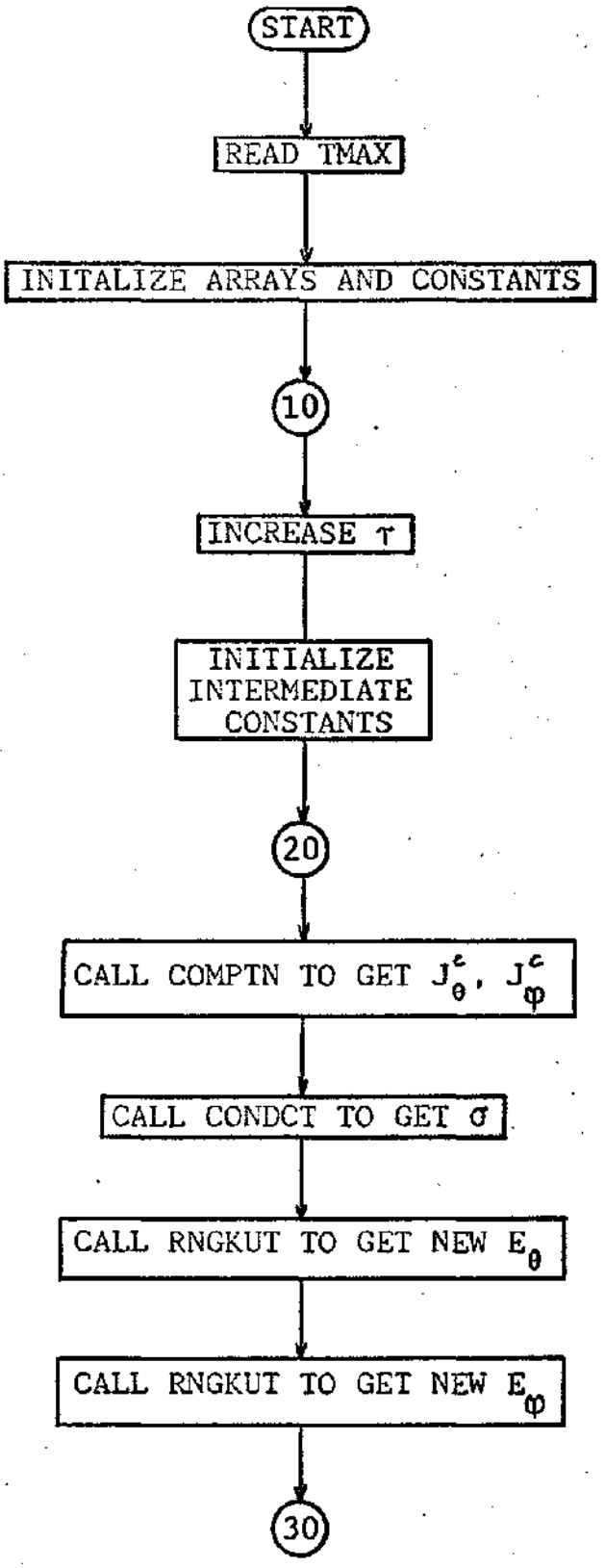
## EMP Code Flow Charts

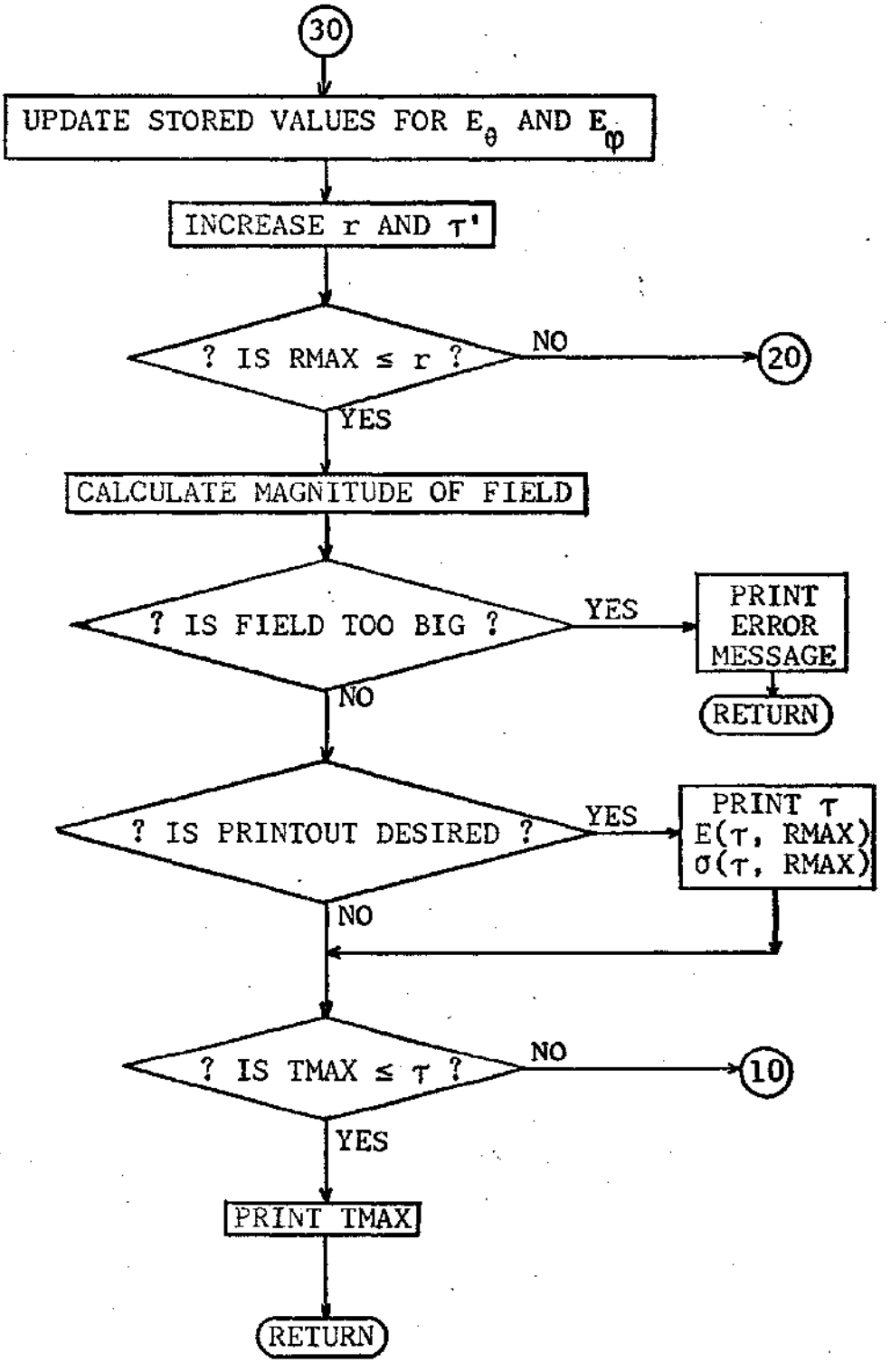
PROGRAM CONTRL



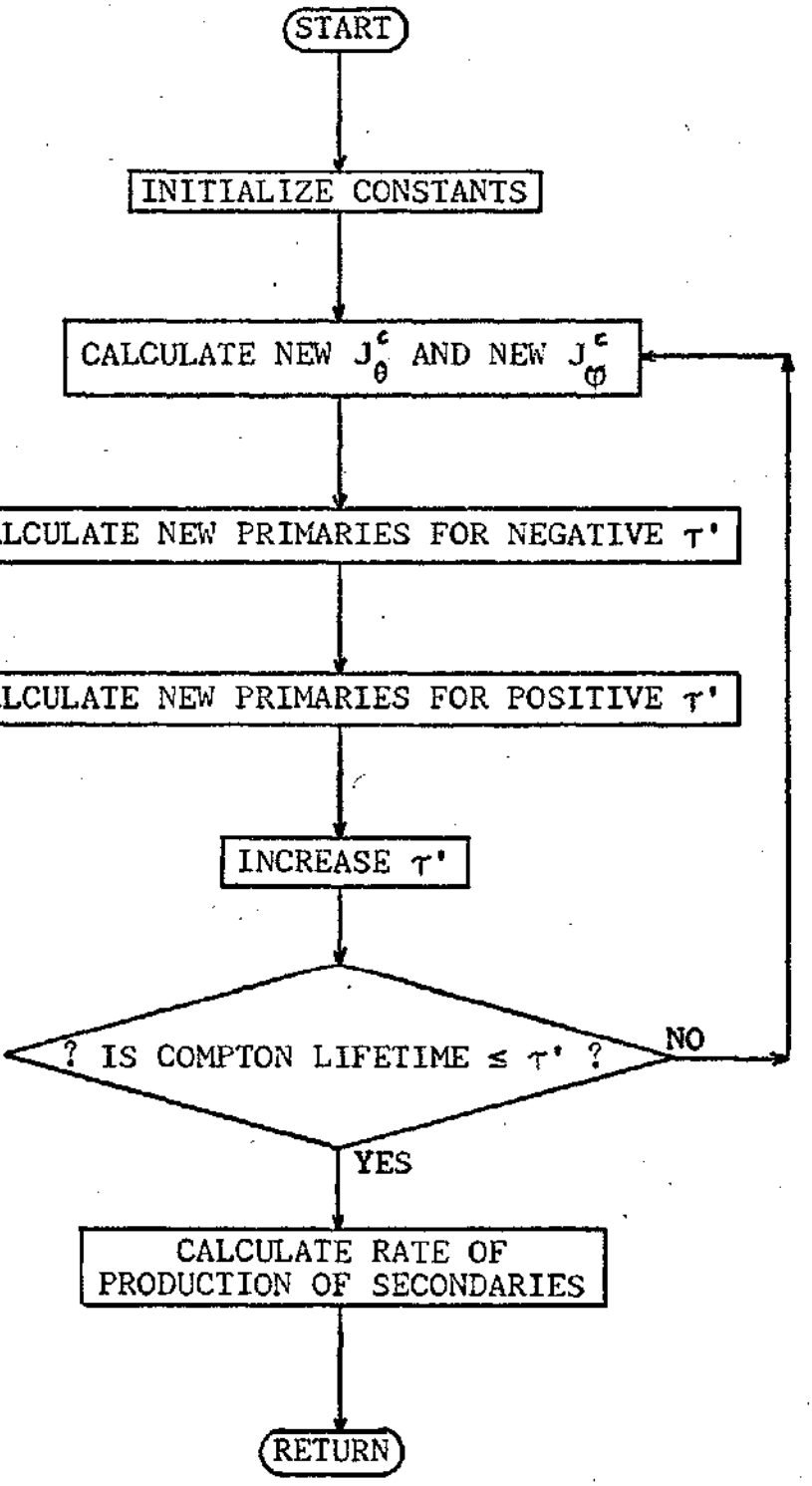

1
CALCULATE ANGLES A AND θ
CALCULATE RMIN AND RMAX
CALL EFIELD TO GET E(τ)
CALCULATE FIELD AT TARGET
SEARCH ARRAY TO FIND PEAK VALUE
PRINT THE TIME PEAK OCCURRED, PEAK VALUE OF FIELD AND THE TIME AND FIELD ARRAYS
? IS PLOT DESIRED ?
YES
CALL ELGPLT
NO
STOP

SUBROUTINE EFIELD

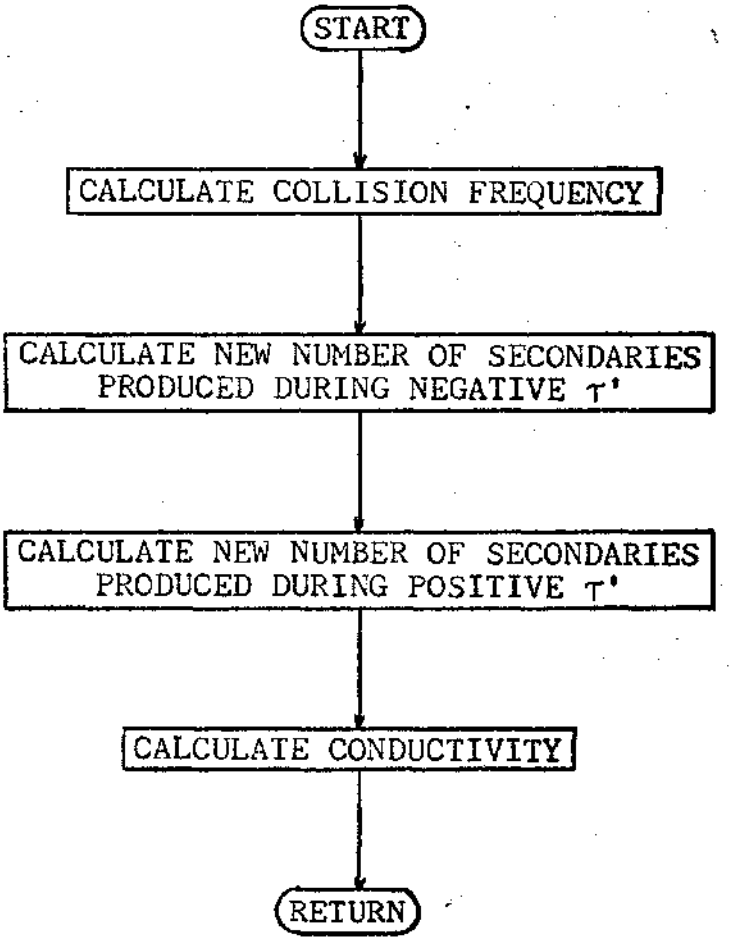



30
UPDATE STORED VALUES FOR $E_\theta$ AND $E_\varphi$
INCREASE r AND τ'
? IS RMAX ≤ r ?
NO
20
YES
CALCULATE MAGNITUDE OF FIELD
? IS FIELD TOO BIG ?
YES
PRINT ERROR MESSAGE
RETURN
NO
? IS PRINTOUT DESIRED ?
YES
PRINT τ
E(τ, RMAX)
σ(τ, RMAX)
NO
? IS TMAX ≤ τ ?
NO
10
YES
PRINT TMAX
RETURN

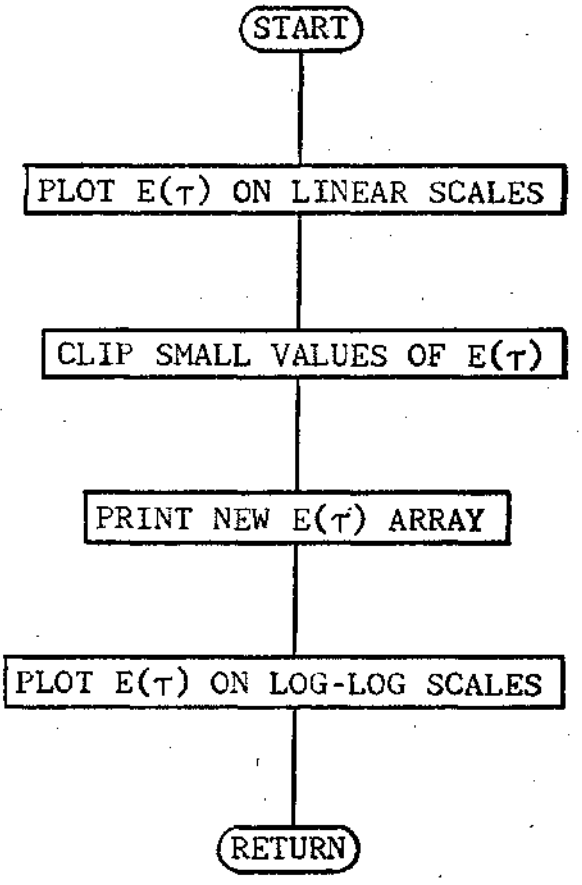
SUBROUTINE COMPTN



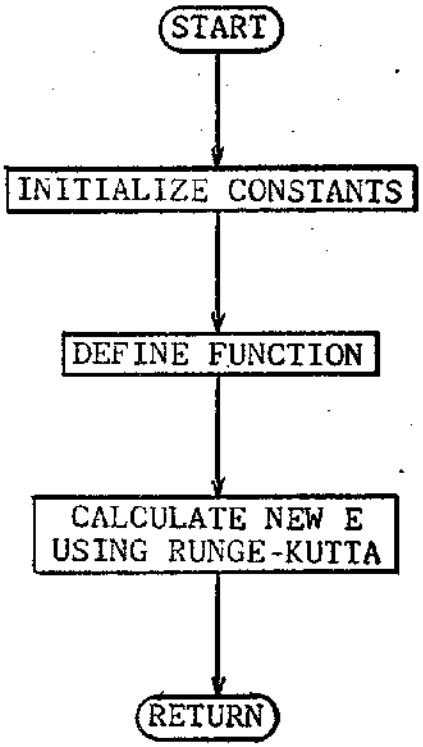
SUBROUTINE CONDCT



SUBROUTINE ELGPLT



SUBROUTINE RNGKUT



# Appendix C

## EMP Code Listing

```
      PROGRAM CONTRL (INPUT,OUTPUT,PLOT)                                CNTL  10
C                                                                       CNTL  20
C         THIS PROGRAM CONTROLS THE SUBROUTINES                         CNTL  30
C                                                                       CNTL  40
      COMMON OUT                                                        CNTL  50
      INTEGER OUT                                                       CNTL  60
      DIMENSION E(192),TIME(192),STORE2(500)                            CNTL  70
C                                                                       CNTL  80
C         X,Y,Z IS THE TARGET LOCATION IN METERS                        CNTL  90
C              FOR THE NORTHERN HEMISPHERE                              CNTL 100
C              X IS MAGNETIC WEST                                       CNTL 110
C              Y IS MAGNETIC SOUTH                                      CNTL 120
C              Z IS ALTITUDE                                            CNTL 130
C                                                                       CNTL 140
C         HOB IS HEIGHT OF BURST IN KILOMETERS >  50KM                  CNTL 150
C                                                                       CNTL 160
C         GAMYLD IS GAMMA YIELD OF BURST IN KILOTONS                    CNTL 170
C                                                                       CNTL 180
C         BFIELD IS THE MAGNITUDE OF EARTHS MAGNETIC FIELD IN THE       CNTL 190
C         ABSORPTION REGION BELOW THE BURST IN WEBERS/SQUARE METER      CNTL 200
C                                                                       CNTL 210
C         BANGLE IS THE DIP ANGLE OF THE MAGNETIC FIELD IN DEGREES      CNTL 220
C                                                                       CNTL 230
C         NDELR IS THE NUMBER OF STEPS BETWEEN RMIN AND RMAX            CNTL 240
C         50<=NDELR<=500                                                CNTL 250
C                                                                       CNTL 260
C         OUT IS THE OUTPUT CONTROL PARAMETER                           CNTL 270
C         OUT=0 ==> PRINT PEAK VALUE AND ARRAYS                         CNTL 280
C         OUT=1 ==> PRINT PEAK VALUE AND MAKE PLOT                      CNTL 290
C         OUT=2 ==> PRINT EVERYTHING AND MAKE PLOT                      CNTL 300
C         OUT=3 ==> PRINT EVERYTHING                                    CNTL 310
C                                                                       CNTL 320
      READ 1001,X,Y,Z,HOB,GAMYLD,BFIELD,BANGLE,NDELR,OUT               CNTL 330
      R=SQRT(X*X+Y*Y+(HOB*1000.-Z)**2)                                  CNTL 340
      PRINT 2006,GAMYLD,HOB,X,Y,Z,R                                     CNTL 350
C                                                                       CNTL 360
```

```
C          SET UP DEFAULT VALUES                                          CNTL 370
C                                                                         CNTL 380
      IF(BANGLE.EQ.0.) BANGLE=40.                                         CNTL 390
      IF(BFIELD.EQ.0.) BFIELD=0.00002                                     CNTL 400
      IF(NDELR.EQ.0) NDELR=50                                             CNTL 410
C                                                                         CNTL 420
C          CONVERT DATA TO MKS UNITS                                      CNTL 430
C                                                                         CNTL 440
      HOB=HOB*1000.                                                       CNTL 450
      GAMYLD=2.61625E25*GAMYLD                                            CNTL 460
      BANGLE=0.017453295*BANGLE                                           CNTL 470
      OMEGA=1.6E-19*BFIELD/(3.505*9.11E-31)                               CNTL 480
C                                                                         CNTL 490
C          PRINT TYPE OF CALCULATION                                      CNTL 500
C                                                                         CNTL 510
      REFLCT=49000.                                                       CNTL 520
      IF(Z.GT.REFLCT)PRINT 2007                                           CNTL 530
      IF(Z.LT.0.0) PRINT 2008                                             CNTL 540
      IF(Z.LE.REFLCT.AND.Z.GE.0.0) PRINT 2009                             CNTL 550
C                                                                         CNTL 560
C          REFLECTED WAVE CALCULATION ASSUMES 100% REFLECTION             CNTL 570
C          AND USES MIRROR IMAGE OF TARGET BELOW GROUND                   CNTL 580
C          SET Z = -Z IF REFLECTED WAVE IS TO BE USED                     CNTL 590
C                                                                         CNTL 600
      IF(Z.GT.REFLCT) Z=-Z                                                CNTL 610
      IF(Z.GT.HOB-1000.) PRINT 2007                                       CNTL 620
      IF(Z.GT.HOB-1000.) Z=-Z                                             CNTL 630
C                                                                         CNTL 640
C          DETERMINE ANGLES                                               CNTL 650
C                                                                         CNTL 660
      R=SQRT(X*X+Y*Y+(HOB-Z)**2)                                          CNTL 670
      A=ACOS((HOB-Z)/R)                                                   CNTL 680
      THETA=ACOS(COS(BANGLE)*Y/R+SIN(BANGLE)*(Z-HOB)/R)                   CNTL 690
C                                                                         CNTL 700
C          DETERMINE RMIN AND RMAX                                        CNTL 710
C                                                                         CNTL 720
```

```
      ZRMIN=5.E4                                                        CNTL 730
      IF(HOB.LT.ZRMIN) ZRMIN=HOB                                        CNTL 740
      TA=(ZRMIN-HOB)/(Z-HOB)                                            CNTL 750
      XRMIN=TA*X                                                        CNTL 760
      YRMIN=TA*Y                                                        CNTL 770
      RMIN=SQRT(XRMIN**2+YRMIN**2+(ZRMIN-HOB)**2)                       CNTL 780
      ZRMAX=Z                                                           CNTL 790
      IF(Z.LT.2.E4) ZRMAX=2.E4                                          CNTL 800
      TB=(ZRMAX-HOB)/(Z-HOB)                                            CNTL 810
      XRMAX=TB*X                                                        CNTL 820
      YRMAX=TB*Y                                                        CNTL 830
      RMAX=SQRT(XRMAX**2+YRMAX**2+(ZRMAX-HOB)**2)                       CNTL 840
C                                                                       CNTL 850
C         CALCULATE EFIELD AT BOTTOM OF ABSORPTION REGION               CNTL 860
C                                                                       CNTL 870
      CALL EFIELD(E,TIME,RMIN,RMAX,NOELR,HOB,A,THETA,OMEGA,GAMYLD,      CNTL 880
     1STORE2)                                                           CNTL 890
C                                                                       CNTL 900
C         CALCULATE EFIELD AT TARGET                                    CNTL 910
C                                                                       CNTL 920
      IF(R.LE.RMAX) GO TO 3                                             CNTL 930
      DO 1 I=1,190                                                      CNTL 940
    1 E(I)=E(I)*RMAX/R                                                  CNTL 950
C                                                                       CNTL 960
C         FIND PEAK VALUE OF EFIELD                                     CNTL 970
C                                                                       CNTL 980
    3 BIG=0.0                                                           CNTL 990
      DO 2 I=1,190                                                      CNTL1000
      IF(E(I).GT.BIG) 4,2                                               CNTL1010
    4 BIG=E(I) $ IT=I                                                   CNTL1020
    2 CONTINUE                                                          CNTL1030
C                                                                       CNTL1040
C         PRINT OUTPUT                                                  CNTL1050
C                                                                       CNTL1060
      PRINT 2010,TIME(IT)                                               CNTL1070
      PRINT 2005,BIG                                                    CNTL1080
```

```
      PRINT 2001                                                        CNTL1090
      PRINT 2002,(TIME(I),I=1,190)                                      CNTL1100
      PRINT 2003                                                        CNTL1110
      PRINT 2004,(E(I),I=1,190)                                         CNTL1120
C                                                                       CNTL1130
CC        IF DESIRED, MAKE PLOT                                         CNTL1140
C                                                                       CNTL1150
      IF(OUT.LE.0.OR.OUT.GE.3) STOP                                     CNTL1160
      CALL ELGPLT (E,TIME,BIG)                                          CNTL1170
      STOP                                                              CNTL1180
 1001 FORMAT(7F10.0,2I5)                                                CNTL1190
 2010 FORMAT(//5X,"PEAK OCCURRED AT",F5.1," SHAKES"//)                  CNTL1200
 2009 FORMAT(5X,"DIRECT WAVE IS BEING CALCULATED"/////)                 CNTL1210
 2008 FORMAT(5X,"REFLECTED WAVE IS BEING CALCULATED"/////)              CNTL1220
 2007 FORMAT(5X,"TARGET IS ABOVE ABSORPTION REGION SO REFLECTED WAVE IS CNTL1230
     1BEING CALCULATED"/////)                                           CNTL1240
 2006 FORMAT("1    THE BURST WITH GAMMA YIELD OF",1PE10.3," KILOTONS"   CNTL1250
     1    /5X,"IS AT AN ALTITUDE OF",1PE10.3," KILOMETERS."            CNTL1260
     2    //5X,"THE TARGET IS AT COORDINATES",3(5X,1PE10.3)            CNTL1270
     3     /5X,"WHICH IS",1PE10.3," METERS FROM THE BURST"/////)        CNTL1280
 2005 FORMAT(//5X,"* * * * * * * * * * * * * * * * * * * * * * * * * *" CNTL1290
     1        /5X,"* PEAK EFIELD AT TARGET IS ",1PE10.3," VOLTS/METER *"CNTL1300
     2        /5X,"* * * * * * * * * * * * * * * * * * * * * * * * * *")CNTL1310
 2004 FORMAT(19(10(3X,1PE10.3)/))                                       CNTL1320
 2003 FORMAT(///5X,"EFIELD VALUES AT TARGET (IN V/M) ARE"//)            CNTL1330
 2002 FORMAT(19(10(4X,F5.1,4X)/))                                       CNTL1340
 2001 FORMAT("1  TIMES USED (IN SHAKES) ARE"//)                         CNTL1350
      END                                                               CNTL1360
```



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```
      SUBROUTINE EFIELD(E,TIME,RMIN,RMAX,NDELR,HOB,A,THETA,OMEGA,GAMYLD,EFLD  10
     1STORE2)                                                              EFLD  20
C                                                                          EFLD  30
C                                                                          EFLD  40
C         CALCULATE THE EFIELD IN THE ABSORPTION REGION                    EFLD  50
C                                                                          EFLD  60
      DIMENSION E(190),TIME(190),STORE2(NDELR)                             EFLD  70
      REAL JTHETA,JPHI                                                     EFLD  80
      INTEGER OUT                                                          EFLD  90
      COMMON OUT,AP,BP,RNP,TOP                                             EFLD 100
C                                                                          EFLD 110
C         ITER IS TIME OF ITERATION IN SHAKES 10<=ITER<=100                EFLD 120
C         READ ITER AND CHANGE IT TO NUMBER OF TIME STEPS                  EFLD 130
C                                                                          EFLD 140
      READ 100,ITER                                                        EFLD 150
      ITER=100+(ITER-10)                                                   EFLD 160
C                                                                          EFLD 170
C         INITIALIZE ARRAYS AND CONSTANTS                                  EFLD 180
C                                                                          EFLD 190
      READ 101,AP,BP,RNP,TOP                                               EFLD 200
  101 FORMAT(4F10.0)                                                       EFLD 210
      DO 61 J=1,100                                                        EFLD 220
      E(J)=0.0 $ TIME(J)=0.1*J                                             EFLD 230
   61 CONTINUE                                                             EFLD 240
      DO 71 J=101,190                                                      EFLD 250
      E(J)=0.0 $ TIME(J)=10.+(J-100.)                                      EFLD 260
   71 CONTINUE                                                             EFLD 270
      DO 51 L=1,NDELR $ STORE2(L)=0.                                       EFLD 280
   51 CONTINUE                                                             EFLD 290
      ETHE=0. $ DELRN=NDELR $ T=0. $ DT=1. $ EPHI=0.                       EFLD 300
      DELTAR=(RMAX-RMIN)/DELRN $ R=RMIN+DELTAR $ RNP=1.E-3*RNP             EFLD 310
C                                                                          EFLD 320
C         START INTEGRATIONS                                               EFLD 330
C         OUTSIDE LOOP IS FOR CALCULATION IN RETARDED TIME                 EFLD 340
C         INSIDE LOOP IS FOR INTEGRATION IN R AT EACH TIME STEP            EFLD 350
C                                                                          EFLD 360
```

```
      DO 21 I=1,190 $ T=T+(1.E-9)*DT $ TIME(I)=T*(1.E8)                    EFLD 370
      IT=I                                                                EFLD 380
      IF(I.GT.ITER) GO TO 42                                              EFLD 390
      TP=-DELTAR/2.88E8$ DTP=TP $ SIGMA=0.$ STORE1=0.                     EFLD 400
      DO 31 K=1,NDELR                                                     EFLD 410
      CALL COMPTN(JTHETA,JPHI,T,R,A,THETA,OMEGA,HOB,GAMYLD,TP,PRI,PRI2)   EFLD 420
      CALL CONDCT(SIGMA,PRI,DTP,DT,HOB,R,A,STORE1,STORE2,K,NDELR,PRI2)    EFLD 430
      CALL RNGKUT(ETHENW,ETHE,R,DELTAR,SIGMA,JTHETA)                      EFLD 440
      CALL RNGKUT(EPHINW,EPHI,R,DELTAR,SIGMA,JPHI)                        EFLD 450
      ETHE=ETHENW $ EPHI=EPHINW $ R=R+DELTAR                              EFLD 460
      TP=TP+DTP                                                           EFLD 470
   31 CONTINUE                                                            EFLD 480
C                                                                         EFLD 490
C         FIND MAGNITUDE OF EFIELD                                        EFLD 500
C                                                                         EFLD 510
      E(I)=SQRT(ETHE**2+EPHI**2)                                          EFLD 520
C                                                                         EFLD 530
C         CHECK FOR DIVERGENCE OF SOLUTION                                EFLD 540
C                                                                         EFLD 550
      IF(E(I).GT.1.E15) GO TO 52                                          EFLD 560
      IF (I.EQ.100) DT=10.                                                EFLD 570
      R=RMIN+DELTAR                                                       EFLD 580
C                                                                         EFLD 590
C         IF DESIRED, PRINT OUTPUT                                        EFLD 600
C                                                                         EFLD 610
      IF (OUT-1.LE.0) GO TO 21                                            EFLD 620
      PRINT 5,I,TIME(I),E(I),SIGMA                                        EFLD 630
   21 CONTINUE                                                            EFLD 640
C                                                                         EFLD 650
C         PRINT MESSAGE AFTER TERMINATION OF TIME LOOP                    EFLD 660
C                                                                         EFLD 670
   42 PRINT 201,TIME(ITER)                                                EFLD 680
      RETURN                                                              EFLD 690
C                                                                         EFLD 700
C         PRINT MESSAGE AFTER ABNORMAL TERMINATION OF TIME LOOP           EFLD 710
C                                                                         EFLD 720
```

```
 52   PRINT 301                                                          EFLC 730
      PRINT 201,TIME(IT)                                                 EFLC 740
      IF(IT.LT.10)RETURN                                                 EFLC 750
C                                                                        EFLC 760
C        SET LAST 5 VALUES OF EFIELD TO 0.0 TO AVOID INCORRECT PEAK      EFLC 770
C                                                                        EFLC 780
      E(IT)=E(IT-1)=E(IT-2)=E(IT-3)=E(IT-4)=E(IT-5)=0.0                  EFLC 790
      RETURN                                                             EFLC 800
 100  FORMAT (I3)                                                        EFLC 810
 5    FORMAT("   I =",I4,"     TIME =",F6.1," SHAKES     E(T,RMAX) =",   EFLC 820
     11PE10.3," VOLTS/METER     SIGMA =",1PE10.3," MHO/METER")           EFLC 830
 201  FORMAT(//5X,"ITERATION TERMINATED AFTER",F5.1," SHAKES"//)         EFLC 840
 301  FORMAT(//15X,"******"/15X,"***** SOLUTION HAS GONE UNSTABLE"       EFLC 850
     1/15X,"******"//)                                                   EFLC 860
      END                                                                EFLC 870
```



```
      SUBROUTINE CONDCT(SIGMA,FFI,DTP,DT,HOB,R,A,STORE1,STORE2,K,NDELR,  CNDT  10
     1FRI2)                                                              CNDT  20
C                                                                        CNDT  30
C        CALCULATES SIGMA AFTER FINDING                                  CNDT  40
C        NSECONDARY FROM NPRIMARY                                        CNDT  50
C                                                                        CNDT  60
C        STORE1 CONTAINS INTEGRAL FOR NEGATIVE TAU                       CNDT  70
C        STORE2 CONTAINS INTEGRAL FOR POSITIVE TAU                       CNDT  80
C                                                                        CNDT  90
      DIMENSION STORE2(NDELR)                                            CNDT 100
      COLISN=4.E12*EXP((R*COS(A)-HOB)/7000.)                             CNDT 110
      STORE1=STORE1-PRI*DTP                                              CNDT 120
      STORE2(K)=STORE2(K)+PRI2*DT*(1.0E-9)                               CNDT 130
      SEC=STORE2(K)-STORE1                                               CNDT 140
      SIGMA=(1.6E-19**2)*SEC/(COLISN*9.11E-31)                           CNDT 150
      RETURN $ END                                                       CNDT 160
```

```
      SUBROUTINE CCMPTN(JTHETA,JPHI,T,R,A,THETA,CMEGA,HOB,GAMYLC,TF,PRI,CMTN  10
     1PRI2)                                                             CMTN  20
C                                                                       CMTN  30
C         CALCULATE THE TWO CCMPCNENTS OF THE                           CMTN  40
C         COMPTON CURRENT AT GIVEN T AND R                              CMTN  50
C         CALCULATE NUMBER OF PRIMARY ELECTRONS                         CMTN  60
C                                                                       CMTN  70
C         JTHETA IS THETA COMPONENT OF COMPTON CURRENT                   CMTN  80
C         JPHI IS PHI COMPONENT OF COMPTON CURRENT                      CMTN  90
C         TMAX IS COMPTON LIFETIME                                      CMTN 100
C         PATH IS ALTITUDE SCALED COMPTON MEAN FREE PATH                CMTN 110
C         TP IS NEGATIVE RETARDED TIME                                  CMTN 120
C         T IS POSITIVE RETARDED TIME                                   CMTN 130
C         PRI IS NUMBER OF PRIMARY ELECTRONS GENERATED DURING TP        CMTN 140
C         PRI2 IS NUMBER OF PRIMARY ELECTRONS GENERATED DURING T        CMTN 150
C         TPRIME IS VARIABLE OF INTEGRATION                             CMTN 160
C                                                                       CMTN 170
C         INITIALIZE CONSTANTS                                          CMTN 180
C                                                                       CMTN 190
      REAL JTHETA,JPHI                                                  CMTN 200
      JTHETA=0. $ JPHI=0. $ TPRIME=(5.E-9) $ TMAX=CLIFE(R,A,HOB)$PRI=0. CMTN 210
      DT=TMAX/10.$ PATH=309.*EXP((HOB-R*COS(A))/7000.)$TPRIME=DT$W=DT/2.CMTN 220
      PRI2=0.                                                           CMTN 230
C                                                                       CMTN 240
C         RUNGE-KUTTA INTEGRATION OF COMPTON CURRENT                    CMTN 250
C                                                                       CMTN 260
      DO 31 K=1,10                                                      CMTN 270
      RK1=DT*CMTHET(HOB,R,A,THETA,CMEGA,PATH,T,TPRIME,GAMYLD)           CMTN 280
      RK2=DT*CMTHET(HOB,R,A,THETA,CMEGA,PATH,T,TPRIME+W,GAMYLD)         CMTN 290
      RK3=RK2                                                           CMTN 300
      RK4=DT*CMTHET(HOB,R,A,THETA,CMEGA,PATH,T,TPRIME+DT,GAMYLD)        CMTN 310
      JTHETA=JTHETA+(RK1+2.*(RK2+RK3)+RK4)/6.                           CMTN 320
      RK5=DT*CMPHI (HOB,R,A,THETA,CMEGA,PATH,T,TPRIME,GAMYLD)           CMTN 330
      RK6=DT*CMPHI (HOB,R,A,THETA,CMEGA,PATH,T,TPRIME+W,GAMYLD)         CMTN 340
      RK7=RK6                                                           CMTN 350
      RK8=DT*CMPHI (HOB,R,A,THETA,CMEGA,PATH,T,TPRIME+DT,GAMYLD)        CMTN 360
```

```
      JPHI=JPHI+(RK5+2.*(RK6+RK7)+RK8)/6.                              CMTN 370
C                                                                      CMTN 380
C         RUNGE-KUTTA INTEGRATION OF PRIMARIES                         CMTN 390
C                                                                      CMTN 400
      RKP1=DT*RKCMTN(R,THETA,OMEGA,TP,TPRIME)                          CMTN 410
      RKP2=DT*RKCMTN(R,THETA,OMEGA,TP,TPRIME+W)                        CMTN 420
      RKP3=RKP2                                                        CMTN 430
      RKP4=DT*RKCMTN(R,THETA,OMEGA,TP,TPRIME+DT)                       CMTN 440
      PRI=PRI+(RKP1+2.*(RKP2+RKP3)+RKP4)/6.                            CMTN 450
      RP1=DT*RKCMTN(R,THETA,OMEGA,T,TPRIME)                            CMTN 460
      RP2=DT*RKCMTN(R,THETA,OMEGA,T,TPRIME+W)                          CMTN 470
      RP3=RP2                                                          CMTN 480
      RP4=DT*RKCMTN(R,THETA,OMEGA,T,TPRIME+DT)                         CMTN 490
      PRI2=PRI2+(RP1+2.*(RP2+RP3)+RP4)/6.                              CMTN 500
      TPRIME=TPRIME+DT                                                 CMTN 510
   31 CONTINUE                                                         CMTN 520
C                                                                      CMTN 530
C         MULTIPLY PRIMARIES BY Q*G(R)/TMAX                            CMTN 540
C         TO OBTAIN RATE OF PRODUCTION OF SECONDARIES                  CMTN 545
C                                                                      CMTN 550
      PRI=PRI*5.000E4*GOFR(R,A,HOB,PATH,GAMYLD)/TMAX                   CMTN 560
      PRI2=PRI2*5.0E4*GOFR(R,A,HOB,PATH,GAMYLD)/TMAX                   CMTN 570
      RETURN $ END                                                     CMTN 580
```

```
      FUNCTION CMPHI(HOB,R,A,THETA,OMEGA,PATH,T,TPRIME,GAMYLD)          CMPH1010
C                                                                       CMPH1020
C         CALCULATES F(T,R) FOR RUNGE-KUTTA INTEGRATION                 CMPH1030
C         OF PHI COMPONENT OF COMPTON CURRENT                           CMPH1040
C                                                                       CMPH1050
      SOLVE=TOFT(T,TPRIME,THETA,OMEGA)                                  CMPH1060
      SOLVE=FOFT(SOLVE)                                                 CMPH1070
      SOLVE=SOLVE*(-4.608E-11)*GCFF(R,A,HOB,PATH,GAMYLD)                CMPH1080
      CMPHI=SOLVE*SIN(THETA)*SIN(OMEGA*TPRIME)                          CMPH1090
      RETURN $ END                                                      CMPH1100
```



```
      FUNCTION CMTHET(HOB,R,A,THETA,OMEGA,PATH,T,TPRIME,GAMYLD)         CMTH1010
C                                                                       CMTH1020
C         CALCULATES F(T,R) FOR RUNGE-KUTTA INTEGRATION                 CMTH1030
C         OF THETA COMPONENT OF COMPTON CURRENT                         CMTH1040
C                                                                       CMTH1050
      SOLVE=TOFT(T,TPRIME,THETA,OMEGA)                                  CMTH1060
      SOLVE=FOFT(SOLVE)                                                 CMTH1070
      SOLVE=SOLVE*(-4.608E-11)*GCFF(R,A,HOB,PATH,GAMYLD)                CMTH1080
      CMTHET=SOLVE*SIN(THETA)*COS(THETA)*(COS(OMEGA*TPRIME)-1.)         CMTH1090
      RETURN $ END                                                      CMTH1100
```

```
      SUBROUTINE RNGKUT (E1,E,R,H,SIGMA,COMPTJ)                          RNKT1010
C                                                                        RNKT1020
C         E(I+1) IS CALCULATED FROM E(I)                                 RNKT1030
C         USING THE RUNGE-KUTTA METHOD                                   RNKT1040
C                                                                        RNKT1050
      DATA (C=3.0E8),(RMUO=12.56637E-7)                                  RNKT1060
      EFUN(R,E)=-(1./R+C*RMUO*SIGMA/2.)*E-COMPTJ*C*RMUO/2.               RNKT1070
      RK1=H*EFUN(R,E)                                                    RNKT1080
      RK2=H*EFUN(R+H/2.,E+RK1/2.)                                        RNKT1090
      RK3=H*EFUN(R+H/2.,E+RK2/2.)                                        RNKT1100
      RK4=H*EFUN(R+H,E+RK3)                                              RNKT1110
      E1=E+(RK1+2.*(RK2+RK3)+RK4)/6.                                     RNKT1120
      RETURN $ END                                                       RNKT1130
```



```
      FUNCTION RKCMTN(R,THETA,OMEGA,TP,TPRIME)                           RKCM1010
C                                                                        RKCM1020
C         CALCULATES F(T) FOR RUNGE-KUTTA                                RKCM1030
C         INTEGRATION OF PRIMARY ELECTRONS                               RKCM1040
C                                                                        RKCM1050
      SOLVE=TOFT(TP,TPRIME,THETA,OMEGA)                                  RKCM1060
      RKCMTN=FOFT(SOLVE)                                                 RKCM1070
      RETURN $ END                                                       RKCM1080
```

```
      FUNCTION GOFR (R,A,HOB,PATH,GAMYLD)                                GOFR1010
C                                                                        GOFR1020
C         SOLVES VIRGIN TRANSPORT AND USES REACTION RATE TO              GOFR1030
C         CALCULATE THE NUMBER DENSITY OF RADIAL ELECTRONS               GOFR1040
C                                                                        GOFR1050
      SOLVE=(.0226275/COS(A))*(-1.+EXP(R*COS(A)/7000.))*EXP(-HOB/7000.)  GOFR1060
      DENOM=12.56637*R*R*PATH*1.E                                        GOFR1070
      GOFR=EXP(-SOLVE)*GAMYLD/DENOM                                      GOFR1080
      RETURN $ END                                                       GOFR1090
```



```
      FUNCTION CLIFE (R,A,HOB)                                           CLIF1010
C                                                                        CLIF1020
C         CALCULATES COMPTON LIFETIME AT RADIUS = R                      CLIF1030
C         MAX ACCEPTABLE LIFETIME = 100 SHAKES FOR                       CLIF1040
C         THE KARZAS-LATTER HIGH FREQUENCY APPROX                        CLIF1050
C                                                                        CLIF1060
      CLIFE=1.04167E-8*EXP((HOE-R*COS(A))/7000.)                         CLIF1070
      IF(CLIFE.GT.1.E-6) CLIFE=(1.E-6)                                   CLIF1080
      RETURN $ END                                                       CLIF1090
```

```
      FUNCTION TOFT (T,TPRIME,THETA,OMEGA)                              TOFT1010
C                                                                       TOFT1020
C        T(T) IS TIME TRANSFORMED TO KARZAS-LATTER FORM                 TOFT1030
C                                                                       TOFT1040
      B=0.958                                                           TOFT1050
      FIRST=T-(1.-B*(COS(THETA)**2))*TPRIME                             TOFT1060
      SECOND=B*(SIN(THETA)**2)*SIN(OMEGA*TPRIME)/OMEGA                  TOFT1070
      TOFT=FIRST+SECOND                                                 TOFT1080
      RETURN $ END                                                      TOFT1090
```



```
      FUNCTION FOFT(T)                                                  FOFT1010
C                                                                       FOFT1020
C        F(T) IS THE POMRANNING MODEL FOR TIME DEPENDENCE               FOFT1030
C        OF NUCLEAR WEAPON YIELD IN RETARDED TIME                       FOFT1040
C                                                                       FOFT1050
      INTEGER OUT                                                       FOFT1060
      COMMON OUT,A,B,RN,TO                                              FOFT1070
      TSHAKE=1.E8*T                                                     FOFT1080
      DENOM=(B+A*EXP((A+B)*(TSHAKE-TO)))*RN                             FOFT1090
      FOFT=(A+B)*EXP(A*(TSHAKE-TO))/DENOM                               FOFT1100
      RETURN $ END                                                      FOFT1110
```

```
      SUBROUTINE ELGPLT(EPLOT,TIME,BIG)                                  EPLT  10
C                                                                        EPLT  20
C         THE FIRST 20 SHAKES OF E(T) IS PLOTTED ON LINEAR SCALES        EPLT  30
C                                                                        EPLT  40
      DIMENSION EPLOT(192),TIME(192) ,E(112),T(112)                      EPLT  50
      MAG = 5 $ SMALL = 0.0                                              EPLT  60
      CHECK = 0.0                                                        EPLT  70
      DO 6 I=1,110                                                       EPLT  80
      E(I)=EPLOT(I) $ T(I)=TIME(I)                                       EPLT  90
    6 CONTINUE                                                           EPLT 100
      CALL PLOT (0.0,-8.0,-3)                                            EPLT 110
      CALL PLOT (2.0,2.0,-3)                                             EPLT 120
      CALL SCALE (T    ,5.,110,1)                                        EPLT 130
      CALL SCALE (E    ,5.,110,1)                                        EPLT 140
      CALL LINE(T    ,E    ,110,1,0,0)                                   EPLT 150
      CALL   AXIS(0.,0.,13HTIME (SHAKES),-13,5.,0.,T    (111),T    (112)) EPLT 160
      CALL   AXIS(0.,0.,12HEFIELD (V/M),12,5.,90.,E    (111),E    (112))EPLT 170
      CALL   AXIS(0.,5.,2H  ,2,5.,0.,T   (111),T   (112))               EPLT 180
      CALL   AXIS(5.,0.,2H  ,-2,5.,90.,E    (111),E    (112))          EPLT 190
      CALL PLOT(10.0,2.0,-3)                                             EPLT 200
C                                                                        EPLT 210
C         SMALL VALUES OF E(T) ARE CLIPPED OFF                           EPLT 220
C         AND E(T) IS PLOTTED ON LOG-LOG SCALES                          EPLT 230
C                                                                        EPLT 240
      DO 3 I=1,190                                                       EPLT 250
      IF((EPLOT(I)/BIG).LT.(10.**(-MAG)))2,3                             EPLT 260
    2 EPLOT(I)=BIG*(10.**(-MAG)) $ CHECK=1.                              EPLT 270
    3 CONTINUE                                                           EPLT 280
      IF(CHECK.EQ.0.) GO TO 11                                           EPLT 290
      PRINT 2005                                                         EPLT 300
      PRINT 2006,(EPLOT(I),I=1,190)                                      EPLT 310
      SMALL=BIG*(10.**(-MAG))                                            EPLT 320
      PRINT 2007,SMALL,BIG                                               EPLT 330
   11 CONTINUE                                                           EPLT 340
      CALL PLOT (0.0,-8.0,-3)                                            EPLT 350
      CALL PLOT (2.0,2.0,-3)                                             EPLT 360
```

```
      CALL LGSCAL (TIME,5.0,190)                                                EPLT 370
      CALL LGSCAL (EPLOT,5.0,190)                                               EPLT 380
      CALL LGLINE (TIME,EPLOT,190,0,0,0)                                        EPLT 390
      CALL LGAXIS(0.,0.,13HTIME (SHAKES),-13,5.,0.,TIME(191),TIME(192))         EPLT 400
      CALL LGAXIS(0.,0.,12HEFIELD (V/M),12,5.,90.,EPLOT(191),EPLOT(192))        EPLT 410
      CALL LGAXIS(0.,5.,2H  ,2,5.,0.,TIME(191),TIME(192))                       EPLT 420
      CALL LGAXIS(5.,0.,2H  ,-2,5.,90.,EPLOT(191),EPLOT(192))                   EPLT 430
      CALL PLOTE                                                                EPLT 440
      RETURN                                                                    EPLT 450
 2005 FORMAT("1    * * * WARNING! PLOT OF E(T) HAS BEEN CLIPPED * * *"/)       EPLT 460
 2006 FORMAT(/5X,"CLIPPED E(T) IS"//19(10(3X,1PE10.3)/))                        EPLT 470
 2007 FORMAT(//"   MINIMUN E(T) IS",1PE10.3/"   MAXIMUM E(T) IS",1PE10.3       EPLT 480
     1)                                                                         EPLT 490
      END                                                                       EPLT 500
```

## Vita

Terry C. Chapman was born on 21 August 1943 in Vancouver, Washington. He graduated from high school in Manitou Springs, Colorado in 1961. He attended the University of Colorado in Boulder where he was elected to Tau Beta Pi, Engineering Honor Society and Sigma Pi Sigma, Physics Honor Society. He received the degree Bachelor of Science, Engineering Physics and a commission in the U. S. Air Force from the University of Colorado in 1969. After attending communications training, he was assigned to Kelly AFB, Texas as a communications operations officer in 1970. He entered the Air Force Institute of Technology in 1972.

Permanent Address: P.O. Box 1144
Manitou Springs, Colorado 80829

This thesis was typed by Ladonna Stitzel.